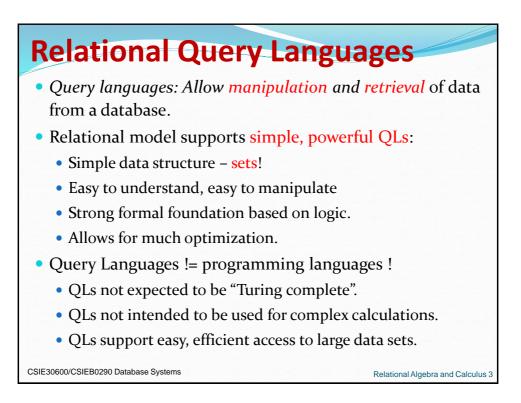
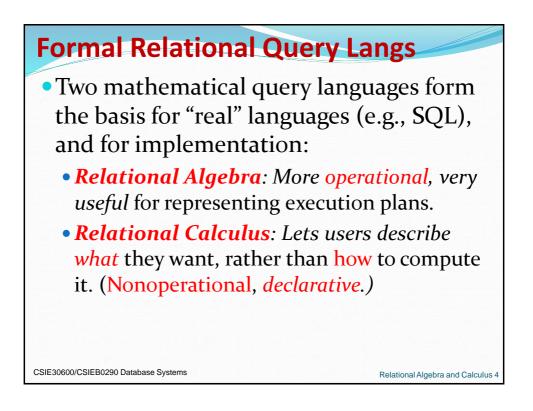
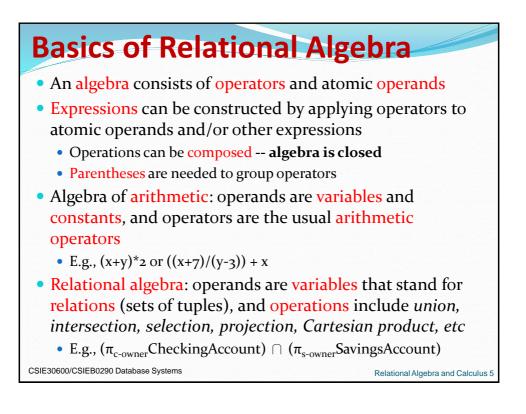
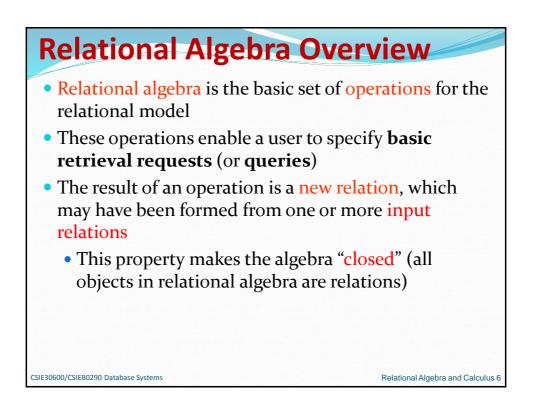


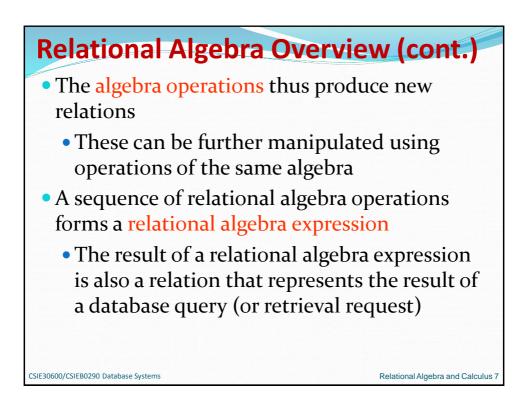
Outline	
Relational Algebra	
<ul> <li>Unary Relational Operations</li> </ul>	
Relational Algebra Operations From	Set Theory
<ul> <li>Binary Relational Operations</li> </ul>	
<ul> <li>Additional Relational Operations</li> </ul>	
• Examples of Queries in Relational Alg	gebra
<ul> <li>Relational Calculus*</li> </ul>	
<ul> <li>Tuple Relational Calculus</li> </ul>	
<ul> <li>Domain Relational Calculus</li> </ul>	
• Example Database Application (COMPA	ANY)
• Overview of the QBE language (append	ix C)*
• (Chapter 8)	
CSIE30600/CSIEB0290 Database Systems	Relational Algebra and Calculus 2

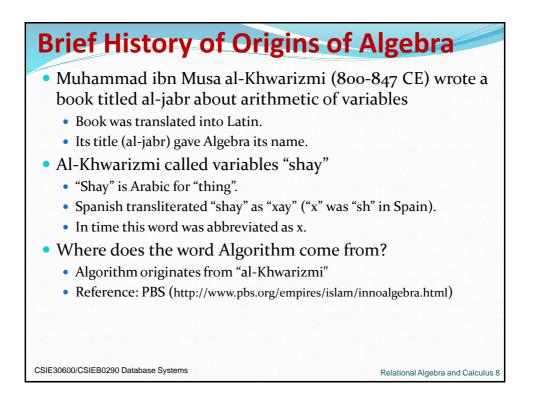


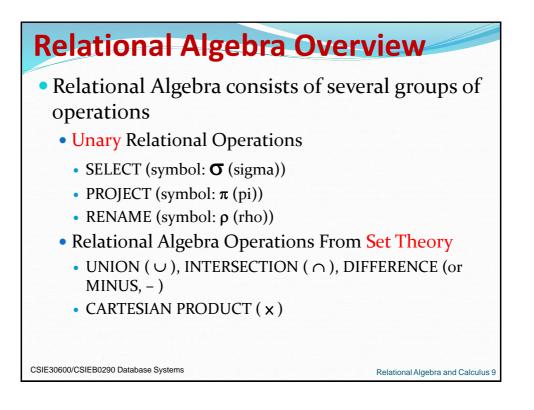


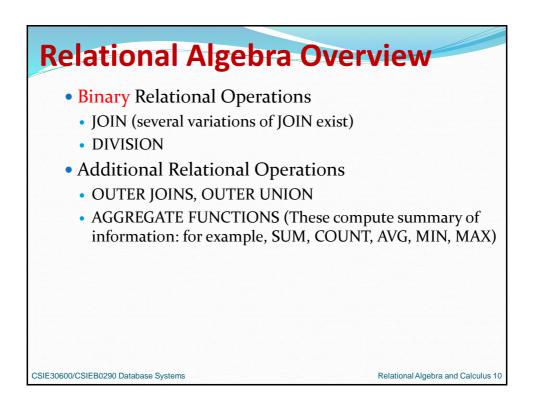








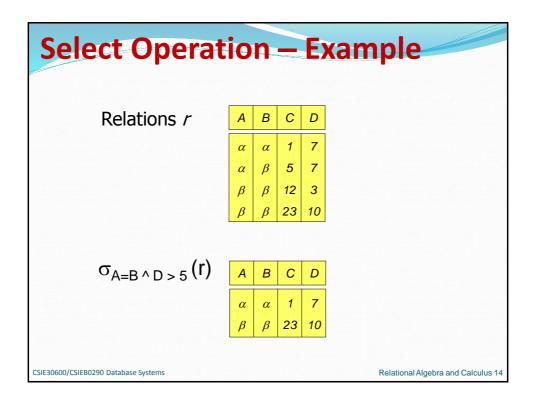


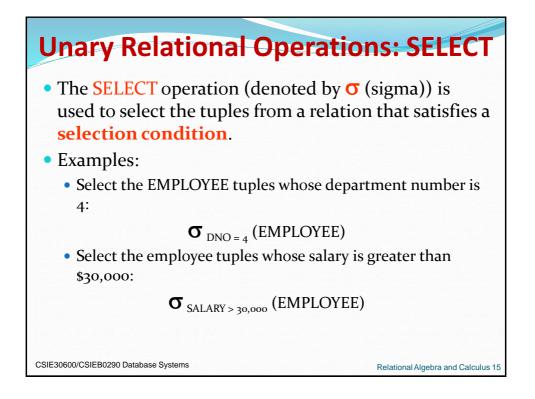


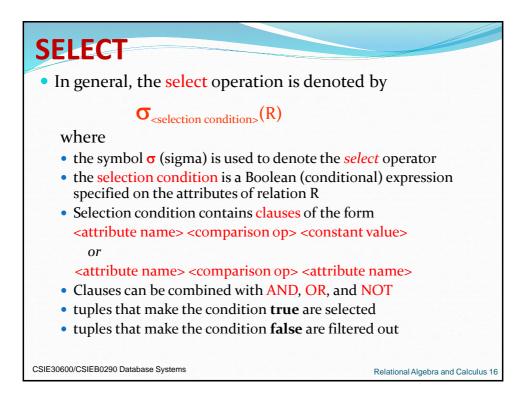
Database State for COMPANY
<ul> <li>Many examples discussed below refer to the COMPANY database shown here.</li> <li>Figure 5.7 Referential integrity constraints displayed on the COMPANY relational database schema.</li> </ul>
EMPLOYEE
Fname         Minit         Lname         Ssn         Bdate         Address         Sex         Salary         Super_ssn         Dno
DEPARTMENT  Dname Dnumber Mgr_ssn Mgr_start_date  DEPT_LOCATIONS  Dnumber Dlocation  PROJECT  Pname Pnumber Plocation Dnum  WORKS_ON
Essn Dependent_name Sex Bdate Relationship
CSIE30600/CSIEB0290 Database Systems Relational Algebra and Calculus 1

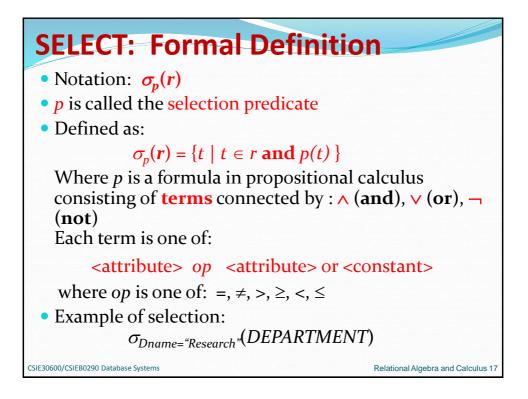
Λα		pie	• •	Jd	ldi	Je	ise s	ιαι	6				
<b>gure 5.6</b> ne possible	e datab	ase state	for the	e COMF	PANY rel	atior	nal database sc	hema.					
EMPLOYE Fname	E	Lname	9	sn	Bdate		Address		Sex	Salary	Super		Dn
John	B	Smith		56789	1965-01		731 Fondren, H	ouston TV	M	30000	33344	_	5
Franklin	T	Wong		45555	1955-12		638 Voss, Hous	M	40000	88866		5	
Alicia	J	Zelaya		87777	1968-01		3321 Castle, S	F	25000	987654		4	
Jennifer	S	Wallace		54321	1941-06		291 Berry, Bella	F	43000	88866		4	
Ramesh	ĸ	Narayan	6668	666884444		9-15	975 Fire Oak. H	M	38000	33344	5555	5	
Joyce	Α	English	4534	53453	1972-07	-31	5631 Rice, Hou	F	25000	33344	5555	5	
Ahmad	V	Jabbar	9879	87987	1969-03-29		980 Dallas, Ho	м	25000	987654	4321	4	
James	E	Borg	8886	65555	1937-11	-10	450 Stone, Houston, TX		м	55000	NULL		1
		1										NC	
DEPARTIN		Dnum	nber	Ma	r_ssn N		lgr_start_date	]		DEPT_C		Dlocat	tion
Researc	sh	5		3334	45555		1988-05-22			1		Houst	on
Adminis	tration	4		9876	54321		1995-01-01			4		Staffo	rd
Headqu	arters	1		8886	65555		1981-06-19	1		5		Bellair	re
		I						1		5		Sugar	land
										5		Houst	on

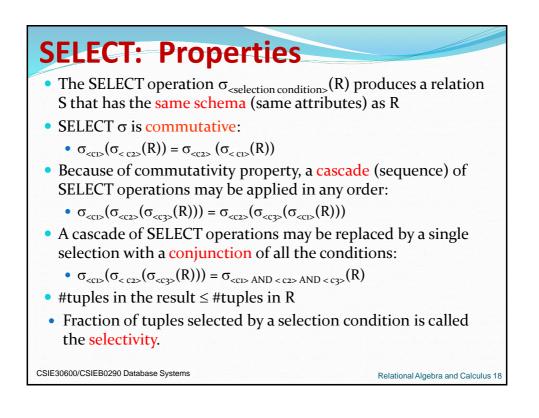
					e sta					
igure 5.6										
ne possibl)	e datal	base stat	te for the COM	IPAN	IY relational	datak	base :	schem	a.	
ORKS_ON					PROJECT					
Essn	Pno	Hours			Pname	Pnu	umber	Plocat	tion	Dnum
123456789	1	32.5			ProductX		1	Bellaire	•	5
123456789	2	7.5			ProductY		2	Sugarla		5
666884444	3	40.0			ProductZ		3	Housto	Houston	
453453453	1	20.0			Computerizatior	1 ·	10	Staffor	d	4
453453453	2	20.0			Reorganization		20	Housto	n	1
333445555	2	10.0			Newbenefits		30	Staffor	d	4
333445555	3	10.0								
333445555	10	10.0	DEPENDENT							
333445555	20	10.0	Essn	De	pendent_name	Sex	Bd	late	Relat	ionship
999887777	30	30.0	333445555	Alic	e	F			-	ghter
999887777	10	10.0	333445555	The	odore	М	1983	3-10-25	Son	-
987987987	10	35.0	333445555	Joy		F			Spouse	
987987987	30	5.0	987654321	Abr	ner	М	1942	2-02-28	Spo	use
987654321	30	20.0	123456789	Mic	hael	М	1988	3-01-04	Son	
987654321	20	15.0	123456789	Alic	e	F	1988	3-12-30	Dau	ghter
888665555	20	NULL	123456789	Fliz	abeth	F	1967	7-05-05	Spo	

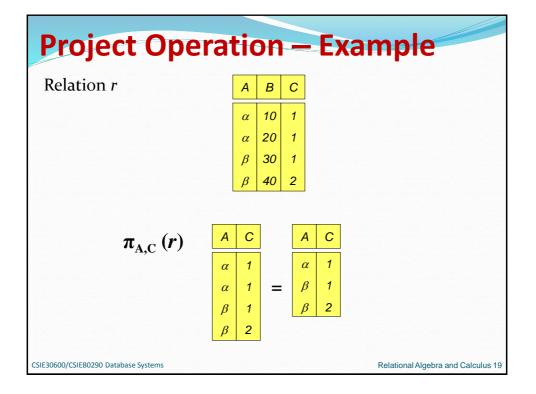


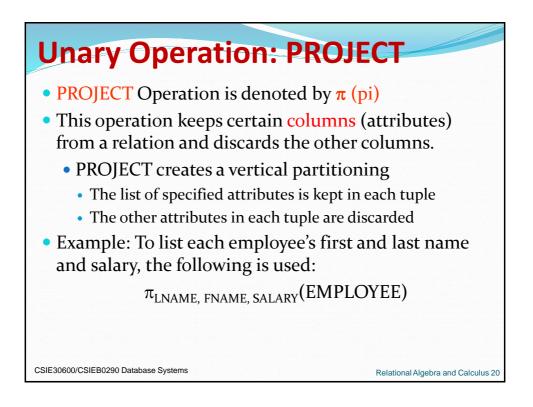


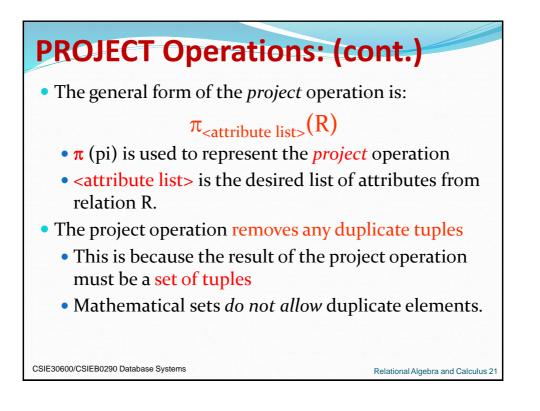


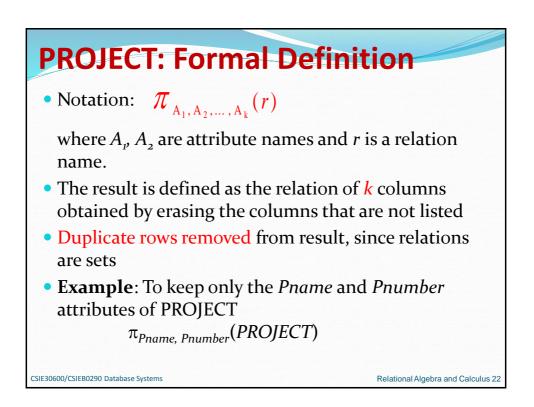


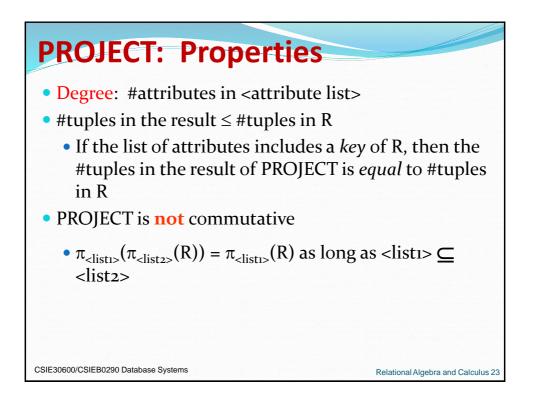




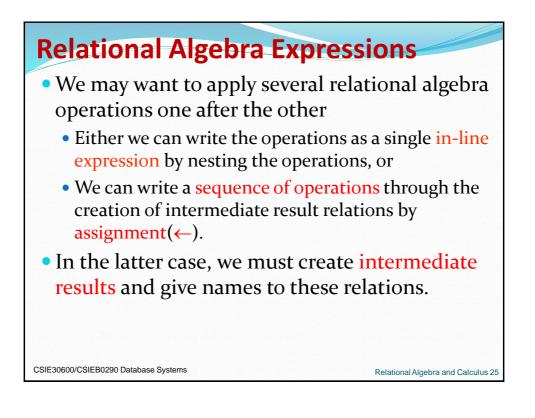


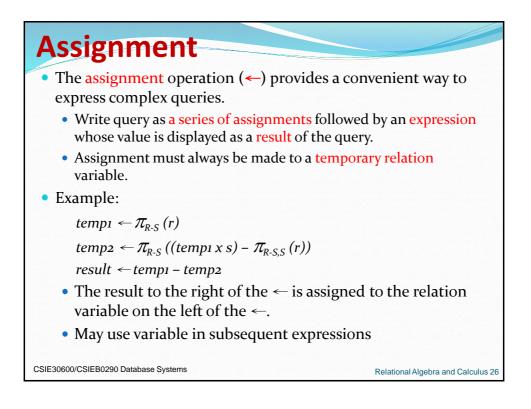


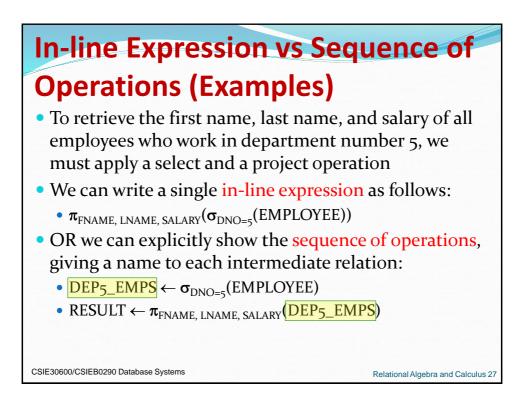


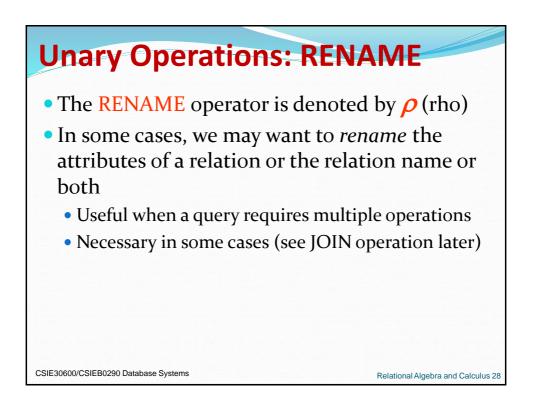


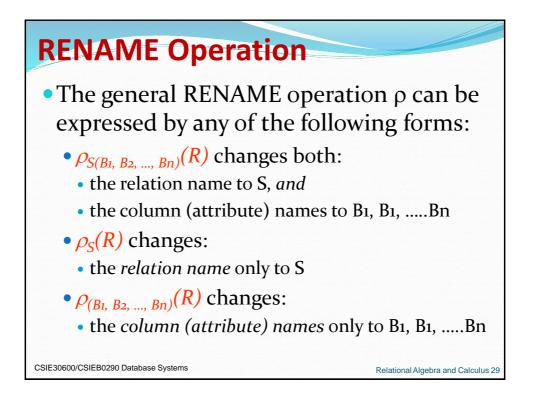
igure 8.1											
esults of S	SELECT	and	I PROJ	ECT opera	tions	(a) $\sigma_{(Dno=}$	4 AND Salary>25000) OR (Dno=	-5 AND	Salary>30	(EMPLC	YEI
) π <sub>Lname, F</sub>	name, Sal	<sub>ary</sub> (E	MPLO	YEE). (c) π	Sex, Sa	alary(EMPL	OYEE).		, outury > or	,000) (	
(a)											
Fname	Minit	Lna	ame	Ssn		Bdate	Address	Sex	Salary	Super_ssn	Dn
Franklin	Т	Wo	ong	33344555	5 19	955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
Jennifer	S	Wa	allace	98765432	1 19	941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Na	rayan	66688444	4 19	962-09-15	975 Fire Oak, Humble, TX	М	38000	333445555	5
					~						
(b)				_	(c)		1				
Lname	Fnan	ne	Salary	<i>(</i>	Sex	Salary					
Smith	John		30000	)	Μ	30000					
Wong	Frank	din	40000	)	М	40000					
Zelaya	Alicia	L I	25000	)	F	25000	1				
Wallace	Jenni	fer	43000	)	F	43000	1				
Narayan	Rame	esh	38000	C	М	38000	1				
English	Joyce	,	25000	)	М	25000	1				
Jabbar	Ahma	ad	25000	)	М	55000					
Jabbar											

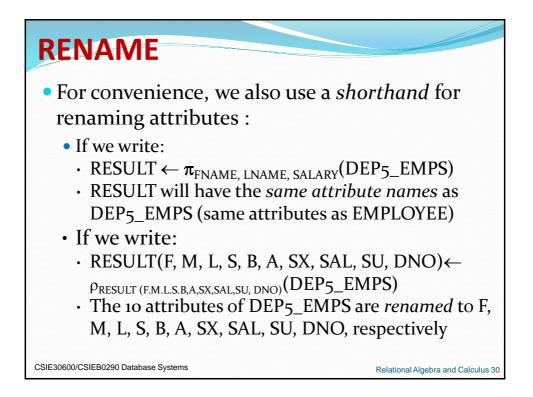




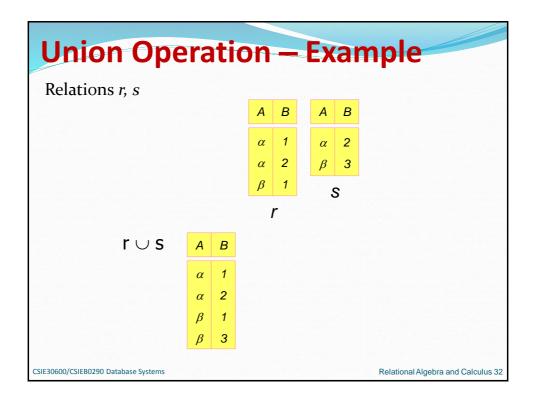


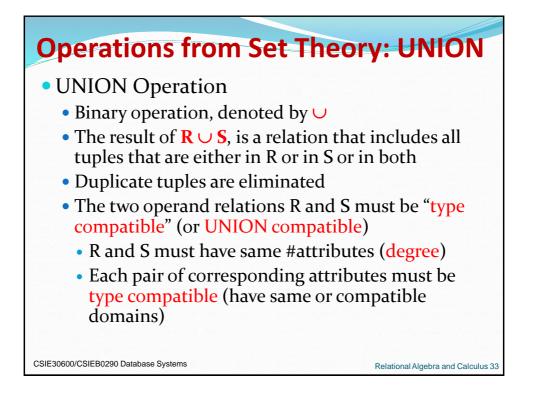


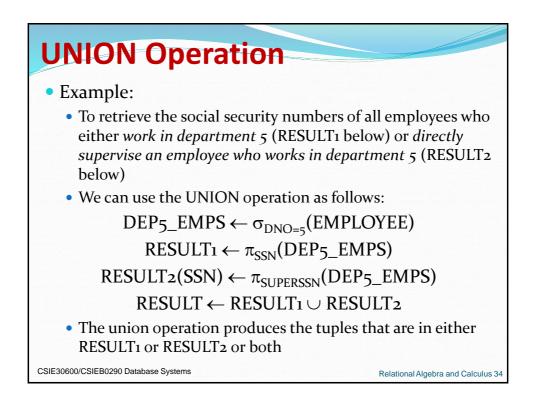


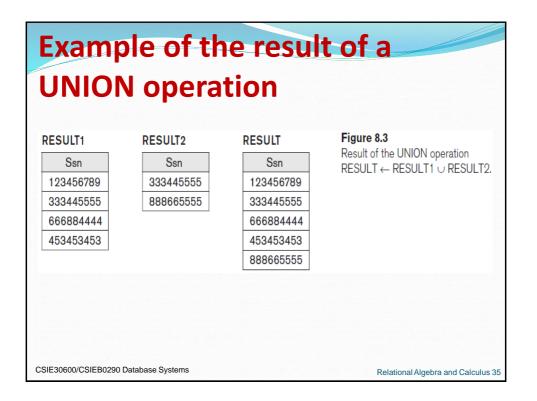


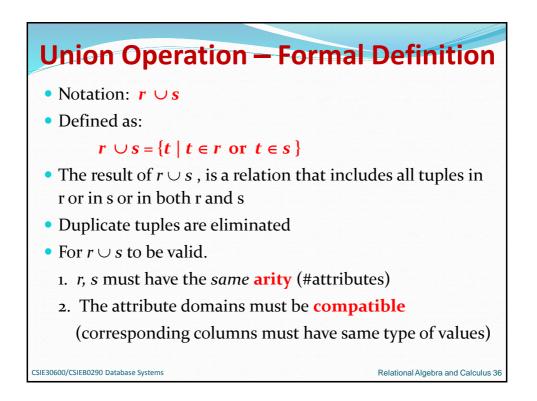
-			-						
Fname	Lname	Salary	_						
John	Smith	30000							
Franklin	Wong								
Ramesh	Naraya		_						
Joyce	English	25000	)						
Fname	Minit	Lname Smith	<u>Ssn</u>	Bdate	Address 731 Fondren, Houston TX	Sex	Salary	Super_ssn 333445555	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston,TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston,TX	М	40000	888665555	5
Ramesh	к	Narayan	666884444	1962-09-15	975 Fire Oak, Humble,TX	M	38000	333445555	5
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
R First_nam John Franklin	le Last Smit Wor Nara	th 3	Salary 30000 40000 38000						
Ramesh									

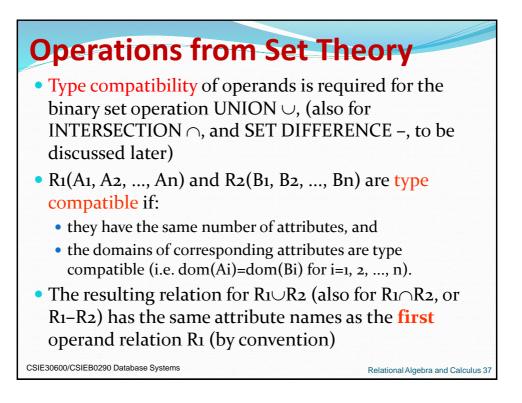


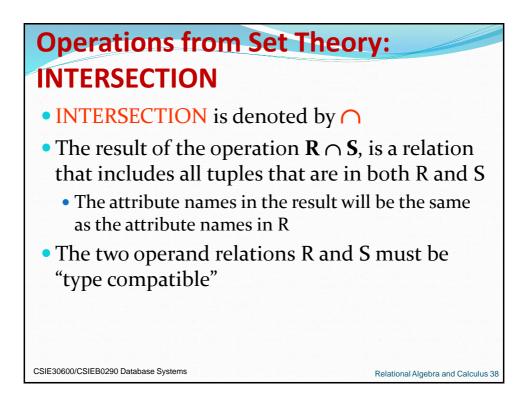


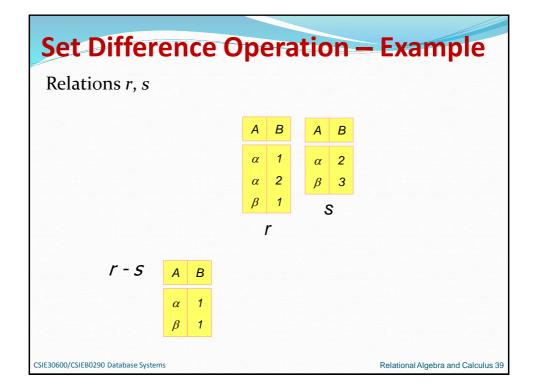


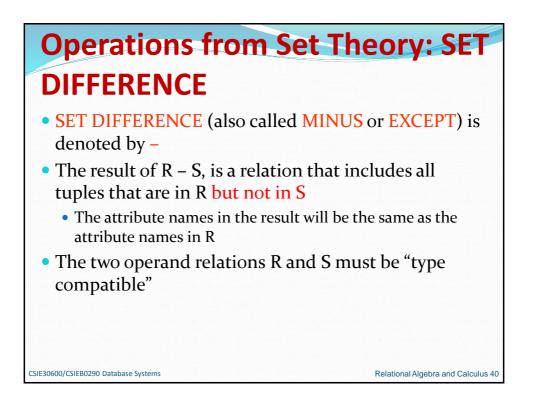


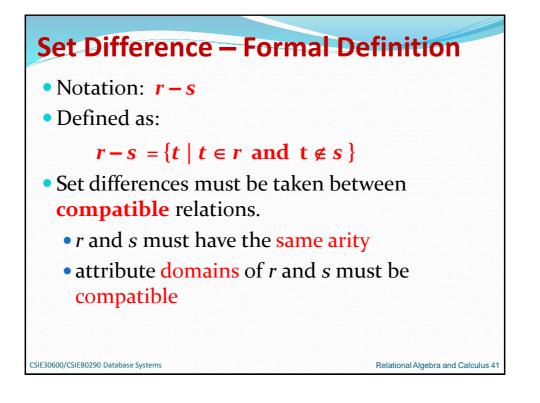


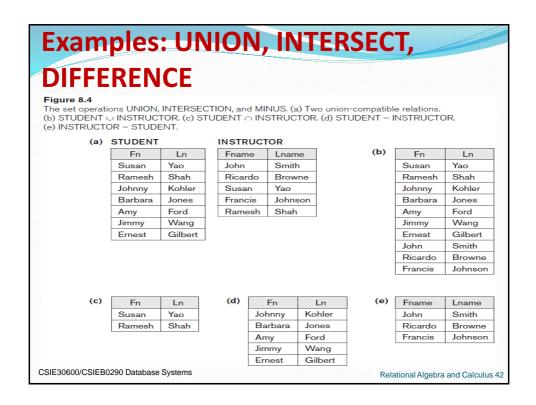


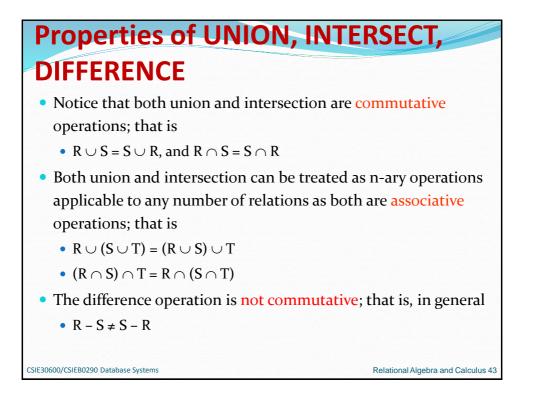


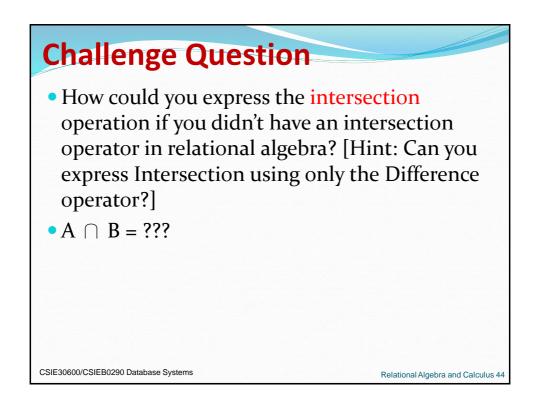


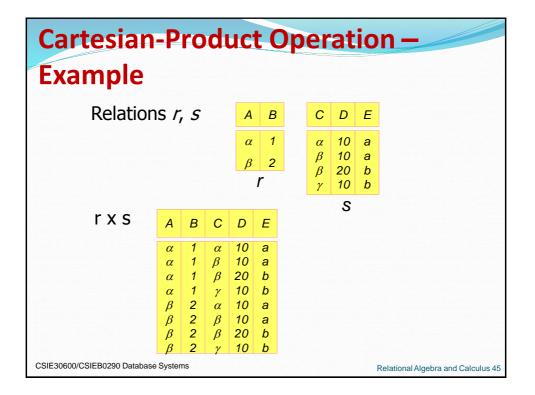


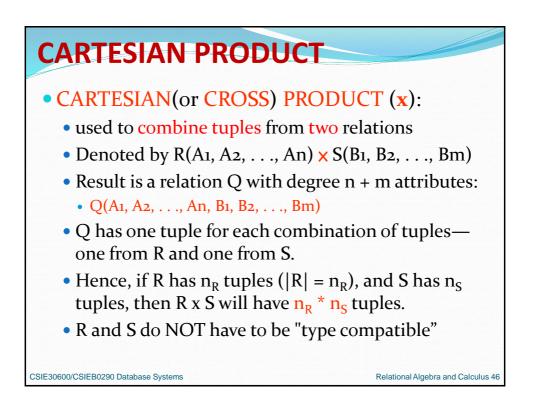




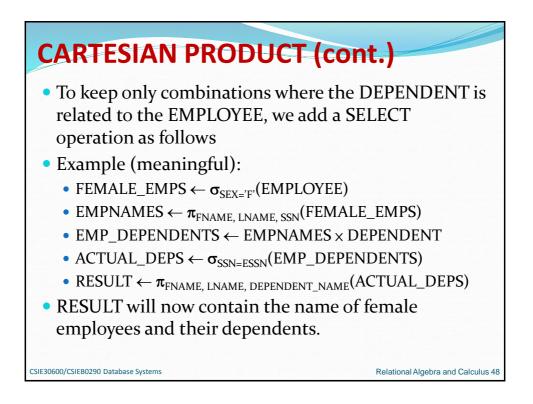




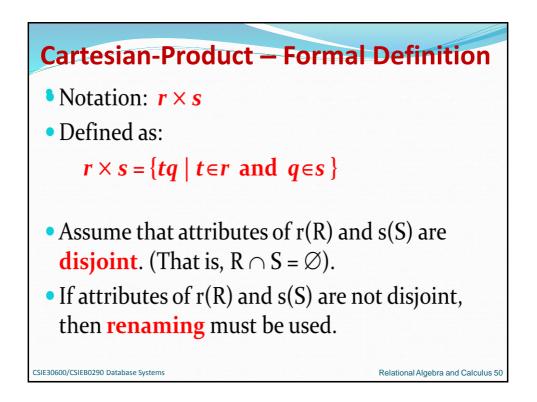


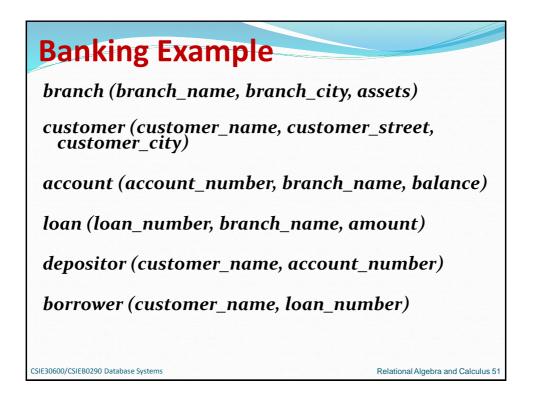


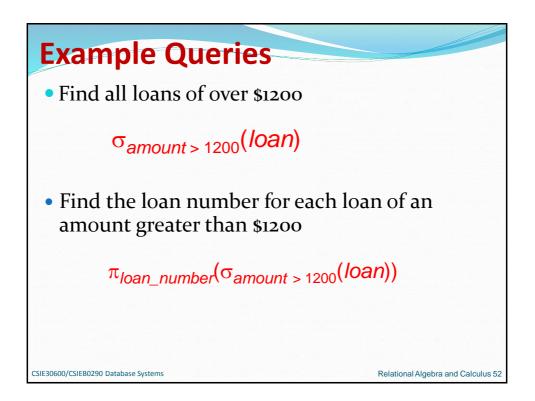


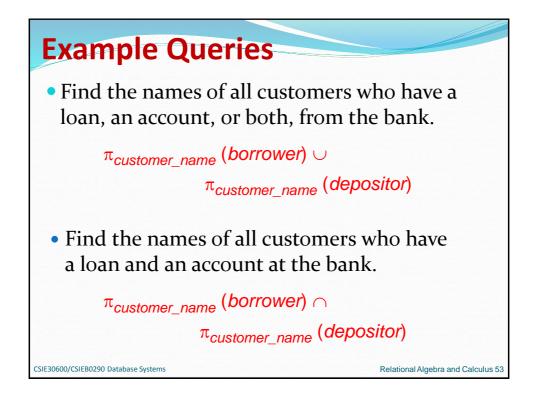


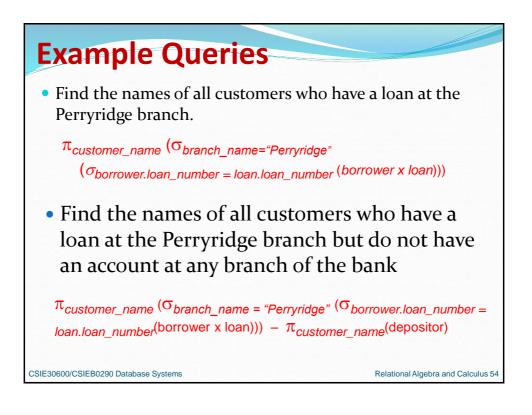
e 8.5											
			(CROSS	PRO	DUCT) of	peratic	n.				
FEMALE											
Fname	Minit	Lname	Ssr		Bdate		Address		Sex	Salary	Super_
Alicia	J	Zelaya	99988		1968-07-		321Castle, Sp		F	25000	987654
Jennifer Joyce	A	Wallace	987654		1941-06-		91Berry, Bellai 631 Rice, Hou		F	43000	888665
		English	45345	3453	1972-07-	31 5	531 Rice, Hou	ston, IA	-	25000	333440
EMPNA				-							
Fname	Lnam		Ssn								
Alicia	Zelay		887777	_							
Jennifer	Walla		654321	-							
Joyce	Englis	sh   453	453453								
EMP_DE	PEND	ENTS									
Fname	Lnam	e :	Ssn	E	ssn	Depe	ndent_name	Sex	Bdate		
Alicia	Zelay	a 9999	387777	3334	445555		Alice	F	1986-04-05		5
Alicia	Zelay	a 999	387777	3334	445555		Theodore	M	198	3-10-25	5
Alicia	Zelay	a 9999	387777	3334	445555		Joy	F	195	8-05-03	3
Alicia	Zelay	a 999	387777	9876	654321		Abner	M	194	2-02-28	3
Alicia	Zelay	a 9999	387777	1234	456789	Michael		M	198	8-01-04	\$
Alicia	Zelay	a 9999	387777	1234	456789		Alice	F	1988-12-30		>
Alicia	Zelay	a 9991	887777	1234	456789		Elizabeth		1967-05-05		5
Jennifer	Walla		354321	333445555			Alice		1986-04-05		5
Jennifer	Walla		354321		445555		Theodore	M			
Jennifer	Walla		354321	3334	445555	Joy		F			3
Jennifer	Walla	0070	354321		354321		Abner	M	194	2-02-28	3
Jennifer	Walla		354321	1234	456789		Michael	M	198	8-01-04	\$
Jennifer	Walla		354321		456789		Alice	F		8-12-30	
Jennifer	Walla		354321		456789		Elizabeth	F		7-05-05	
Joyce	Englis		453453		445555		Alice	F		86-04-05	
Joyce	Englis		453453		445555		Theodore	M		3-10-25	
Joyce	Englis		453453		445555		Joy	F		8-05-03	
Joyce	Englis		453453		354321		Abner	M		2-02-28	
Joyce	Englis		453453		456789		Michael	M		8-01-04	
Joyce	Englis		453453		456789		Alice	F		8-12-30	
Joyce	Englis	sh   4534	453453	1234	456789		Elizabeth	F	196	\$7-05-05	
ACTUAL	DEPE	NDENT	5								
Fname	Lnam	e :	Ssn	Es	ssn	Depe	ndent_name	Sex	E	Bdate	
Jennifer	Walla	ce 9876	654321	9876	654321		Abner	M	194	2-02-28	3
RESULT											
Ename	Lnam	e Dep	endent_n	ame							

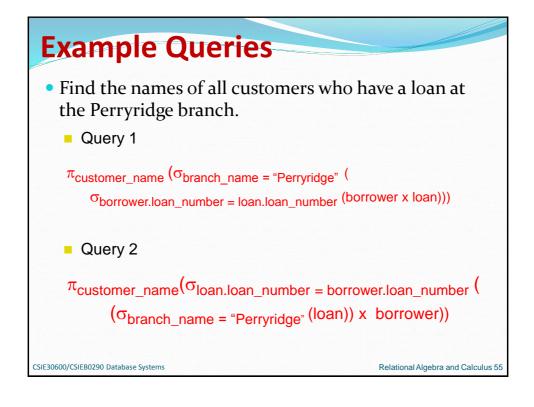


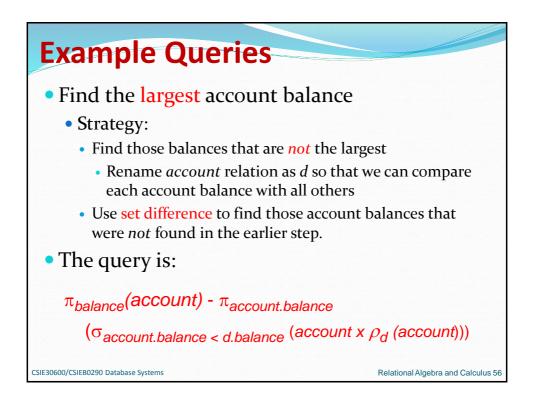


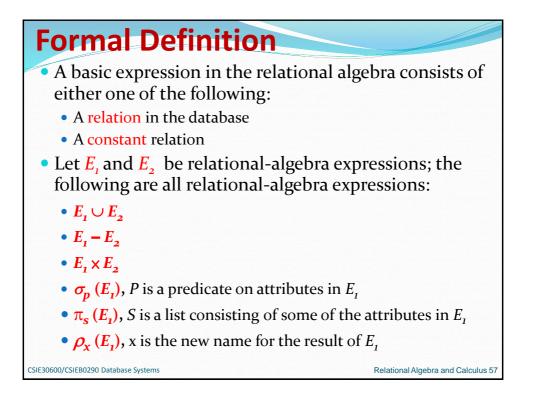


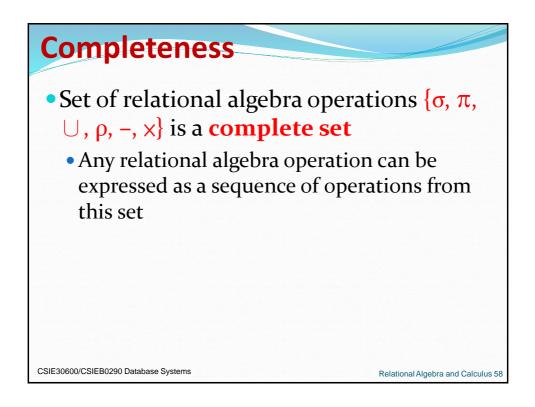


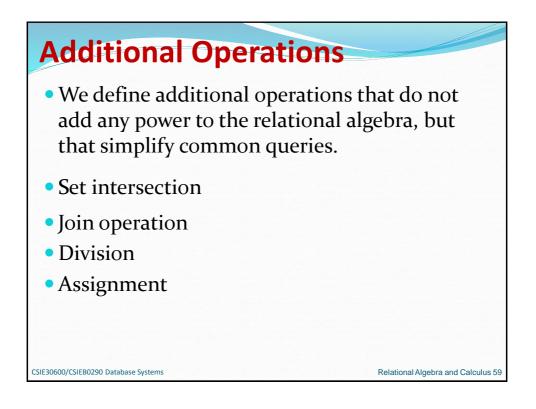


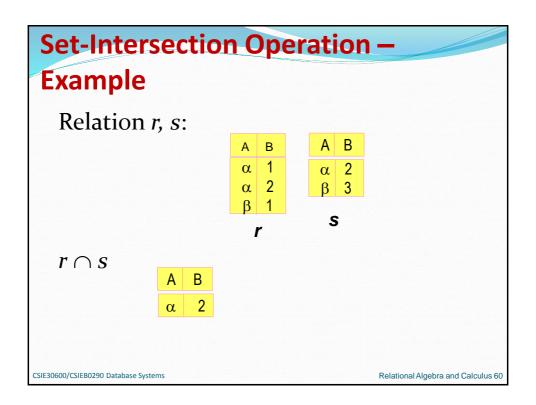


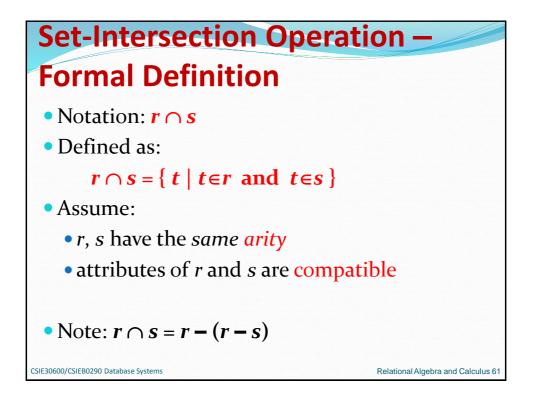


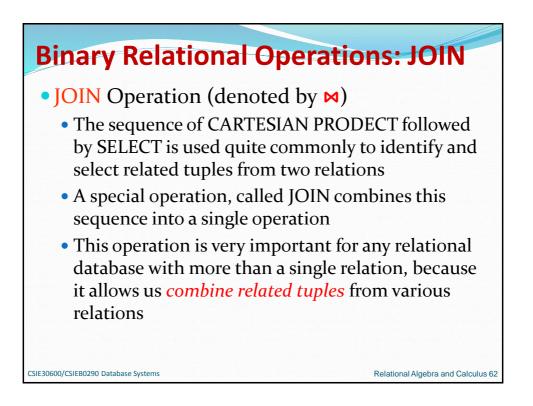


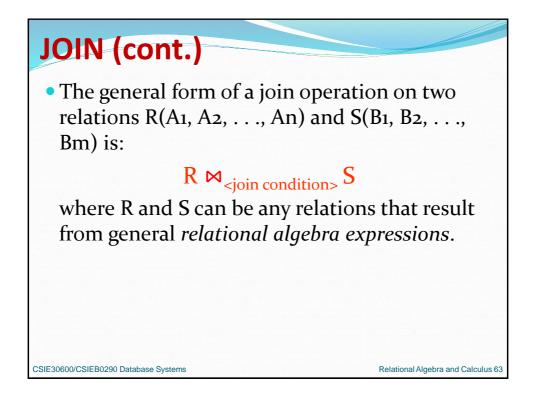


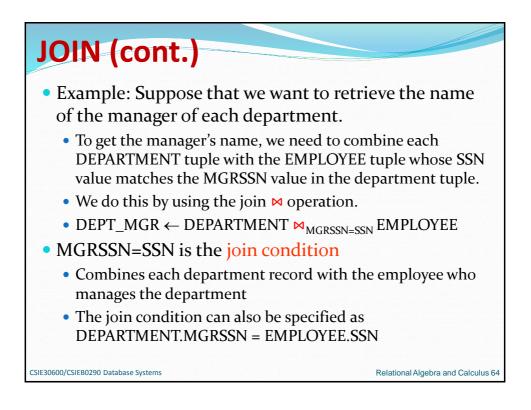






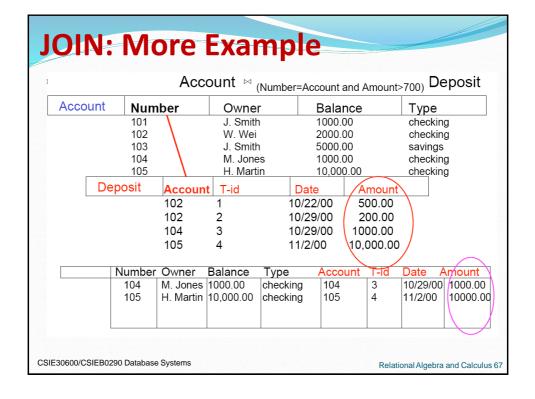


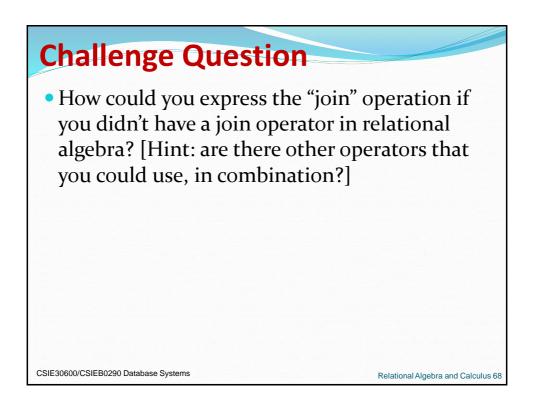


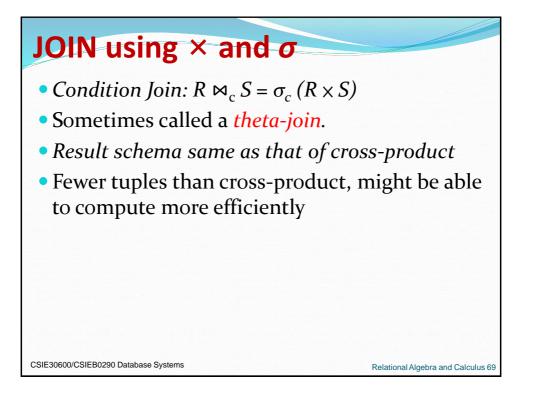


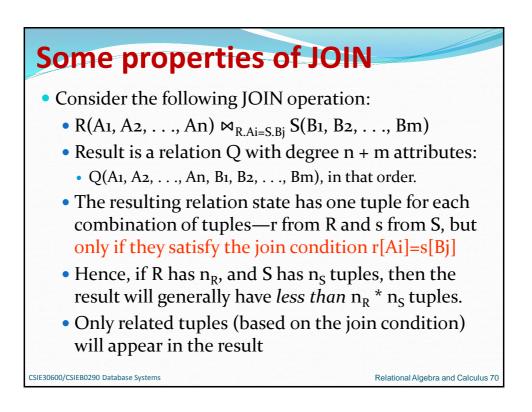
gure 8.6								
sult of the JOIN	operation DE	$PT_MGR \leftarrow DEF$	PARTME	ENT⊠ <sub>Mgr_ss</sub>	<sub>in=Ssn</sub> EM	PLOYEE.		
DEPT_MGR								
Dname	Dnumber	Mgr_ssn		Fname	Minit	Lname	Ssn	
Research	5	333445555		Franklin	Т	Wong	333445555	
Administration	4	987654321		Jennifer	S	Wallace	987654321	
Headquarters	1	888665555		James	Е	Borg	888665555	

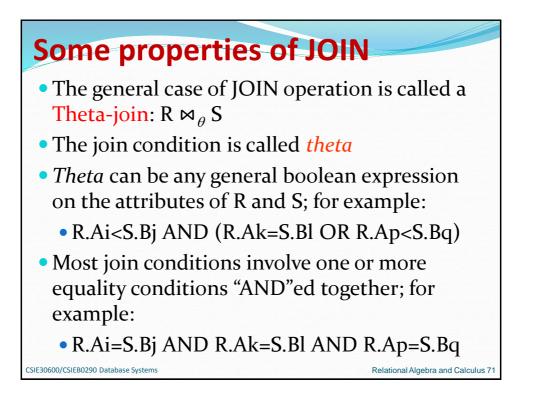
011	N: M	Nor	еE	Xa	am	pl	e						
	$\bowtie$	= join			Acc	ou	nt ⋈	Num	ber=Acco	<sub>unt</sub> De	posit		
Acco	ount	Numbe	r	Owner			Balance			Туре			
		101		J. S	Smith		10	00.00	)	chec	king		
		102		W. Wei 20			20	00.00	)	chec	checking		
		103		J. 8	Smith		50	00.00	)	savin	gs		
		104	\	Μ.	Jones		10	00.00	)	checl	king		
		105	1	Η.	Martin		10	,000.	00	checl	king		
	Deposit		count	Tran	saction-	·id	Date		Amoun	t	-		
		10	2	1		1	0/22/0	0	500.00				
		10	2	2		1	0/29/0	0	200.00				
		10	4	3		1	0/29/0	0	1000.00				
		10	5	4		1	1/2/00	-	10,000.0	0			
	Number	Owner	Balance	e T	уре	Acc	count T	rans	action-id	Date	Amount		
	102	W. Wei	2000.00	) (	checking		102	1		10/22/00	500.00		
	102	W. Wei	2000.00	) (	checking		102	2		10/29/00	200.00		
	104	M. Jones	1000.00	) (	checking		104	3		10/29/00	1000.00		
	105	H. Martin	10,000.	00 o	checking		105	4		11/2/00	10000.00		
IE30600/CS	SIEB0290 Da	atabase Syste	ms						Relatio	onal Algebra	a and Calculu		

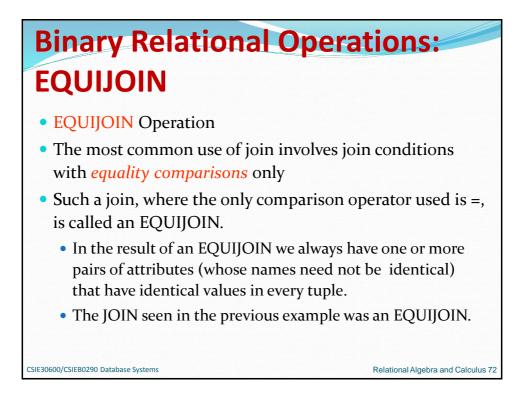




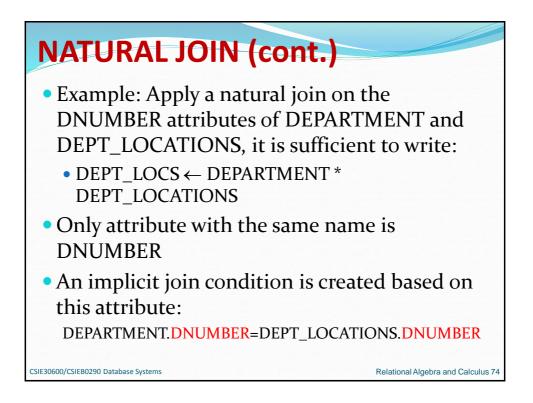


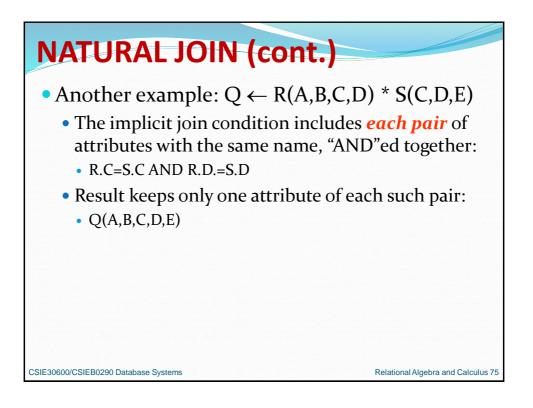




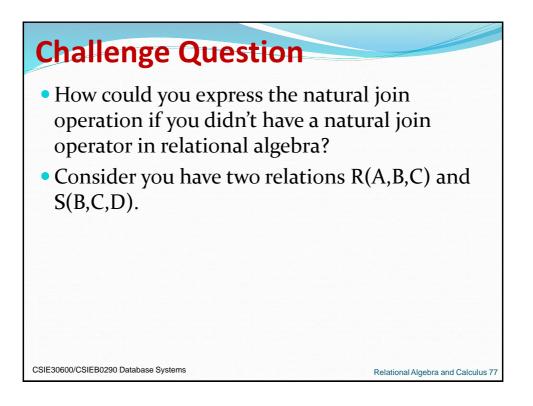


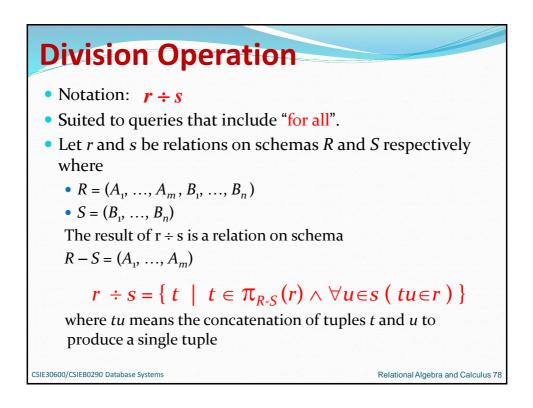


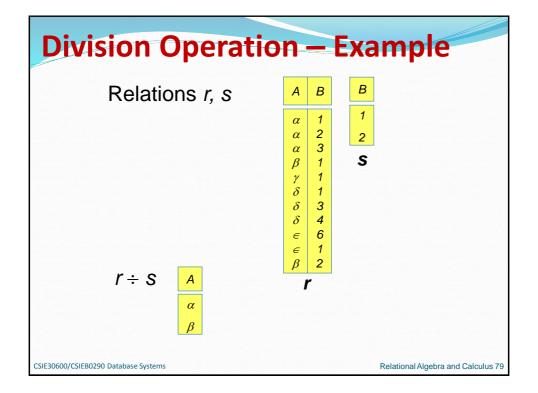


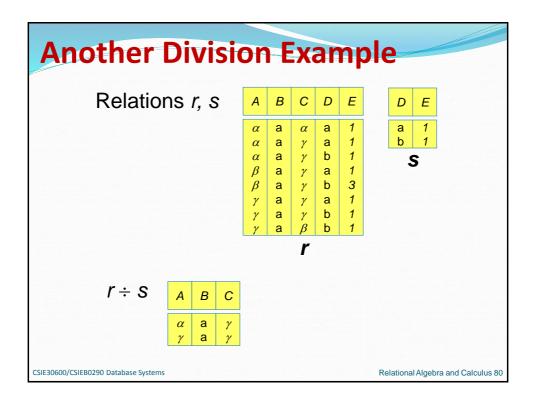


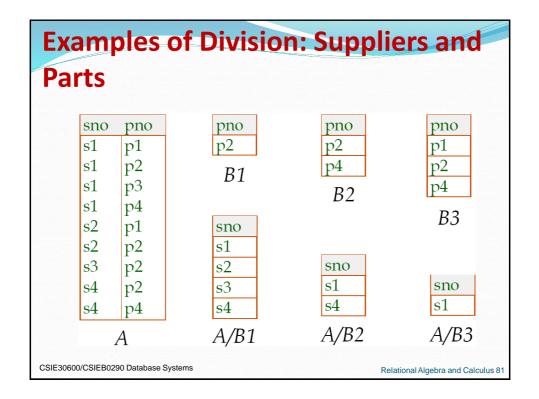
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ProductY	2	Sugarland	5	Research	333445555	1988-05-22
ProductZ	3	Houston	5	Research	333445555	1988-05-22
Computerization	10	Stafford	4	Administration	987654321	1995-01-01
Reorganization	20	Houston	1	Headquarters	888665555	1981-06-19
Newbenefits			Stafford 4 Administration			
b)	30	Stafford	4	Administration	987654321	1995-01-01
b) )EPT_LOCS						1995-01-01
b) DEPT_LOCS Dname	Dnumber	Stafford Mgr_ssn 888665555	Mgr	r_start_date	Location	1995-01-01
b) )EPT_LOCS		Mgr_ssn	Mgr 198	r_start_date   31-06-19		1995-01-01
b) DEPT_LOCS Dname Headquarters	Dnumber 1	Mgr_ssn 888665555	Mgr 198	r_start_date   31-06-19   95-01-01	Location Houston	1995-01-01
b) DEPT_LOCS Dname Headquarters Administration	Dnumber 1 4	Mgr_ssn 888665555 987654321	Mgr 198 199	r_start_date   31-06-19   95-01-01   38-05-22	Location Houston Stafford	1995-01-01
) EPT_LOCS Dname Headquarters	Dnumber 1	Mgr_ssn 888665555	Mgr 198	r_start_date   31-06-19	Location Houston	1995-01-01
b) DEPT_LOCS Dname Headquarters Administration Research	Dnumber 1 4 5	Mgr_ssn 888665555 987654321 333445555	Mgr 198 199	r_start_date   31-06-19   95-01-01   38-05-22	Location Houston Stafford Bellaire	1995-01-01











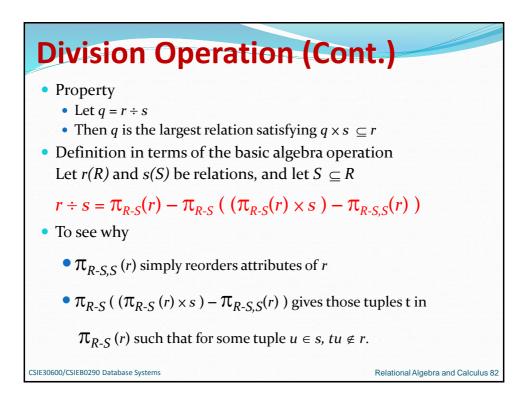
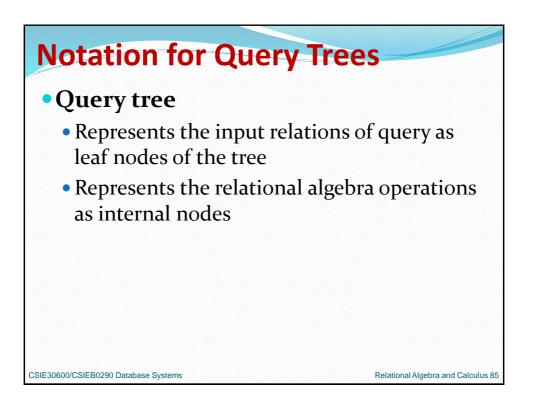
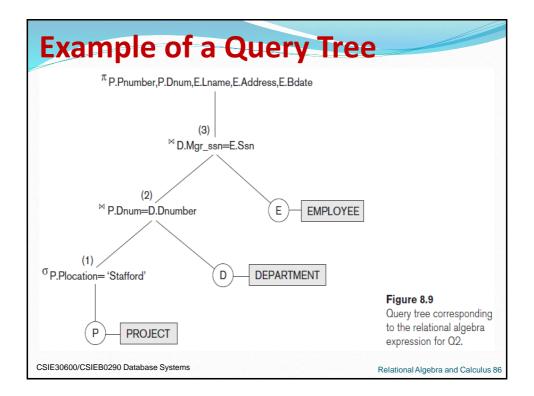
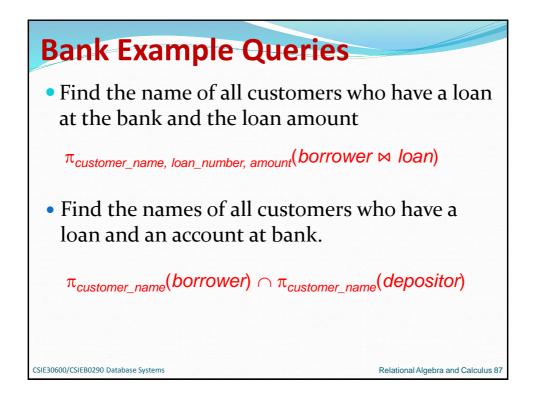


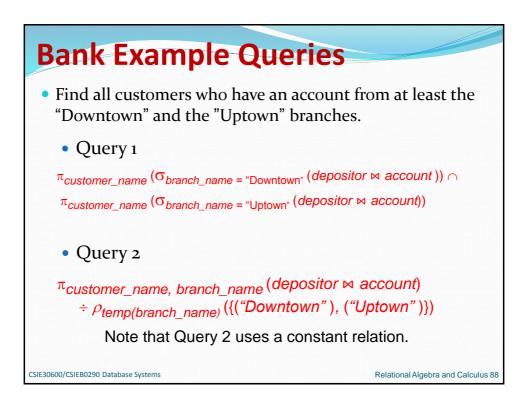
Table 0.4 O		
Table 8.1 Operation	ns of Relational Algebra	
OPERATION	PURPOSE	NOTATION
SELECT	Selects all tuples that satisfy the selection condition from a relation <i>R</i> .	$\sigma_{< \text{selection condition}>}(R)$
PROJECT	Produces a new relation with only some of the attributes of <i>R</i> , and removes duplicate tuples.	$\pi_{< attribute \ list>}(R)$
THETA JOIN	Produces all combinations of tuples from $R_1$ and $R_2$ that satisfy the join condition.	$R_1 \bowtie_{<\text{join condition}>} R_2$
Equijoin	Produces all the combinations of tuples from $R_1$ and $R_2$ that satisfy a join condition with only equality comparisons.	$\begin{array}{l} R_1 \bowtie _{<\text{join condition}>} R_2, \text{OR} \\ R_1 \bowtie _{(<\text{join attributes 1>}),} \\ _{(<\text{join attributes 2>})} R_2 \end{array}$
NATURAL JOIN	Same as EQUIJOIN except that the join attributes of $R_2$ are not included in the resulting relation; if the join attributes have the same names, they do not have to be specified at all.	$\begin{array}{l} R_1 *_{<\text{join condition}>} R_2,\\ \text{OR } R_1 *_{(<\text{join attributes 1>}),}\\ (<\text{join attributes 2>})\\ R_2 \text{ OR } R_1 * R_2 \end{array}$
SIE30600/CSIEB0290 Databas	e Systems	Relational Algebra and Calculus

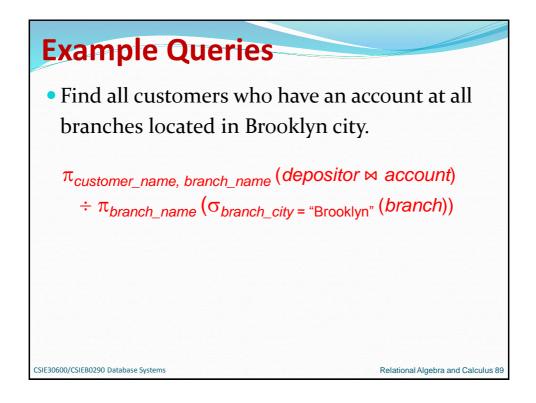
UNION	Produces a relation that includes all the in $R_1$ or $R_2$ or both $R_1$ and $R_2$ ; $R_1$ and $R_2$ ; be union compatible.	1	$R_1 \cup R_2$
INTERSECTION	Produces a relation that includes all the in both $R_1$ and $R_2$ ; $R_1$ and $R_2$ must be un compatible.		$R_1 \cap R_2$
DIFFERENCE	Produces a relation that includes all the in $R_1$ that are not in $R_2$ ; $R_1$ and $R_2$ must union compatible.	1	$R_1 - R_2$
CARTESIAN PRODUCT	Produces a relation that has the attribute $R_1$ and $R_2$ and includes as tuples all possions combinations of tuples from $R_1$ and $R_2$ .		$R_1 \times R_2$
DIVISION	Produces a relation $R(X)$ that includes a $t[X]$ in $R_1(Z)$ that appear in $R_1$ in combinities with every tuple from $R_2(Y)$ , where $Z =$	nation	$R_1(Z) \div R_2(Y)$
CSIE30600/CSIEB0290 Database S	ystems	Relational Alge	bra and Calculus 84

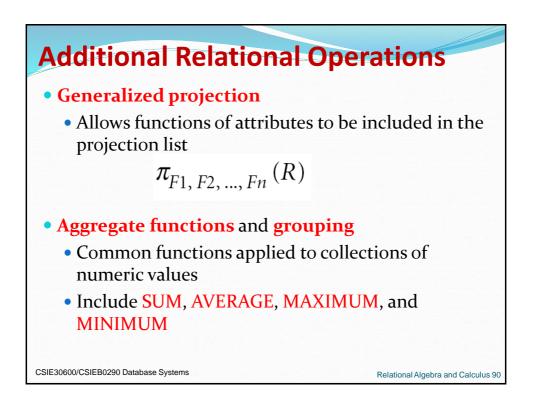


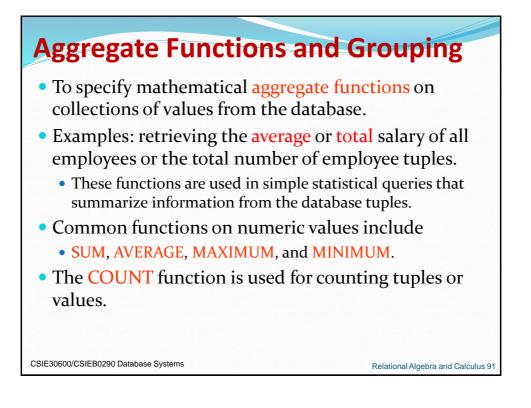


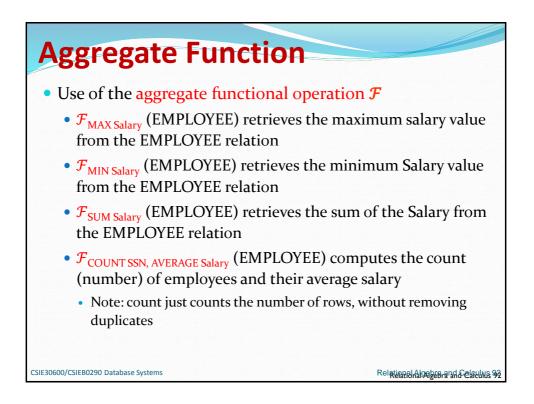


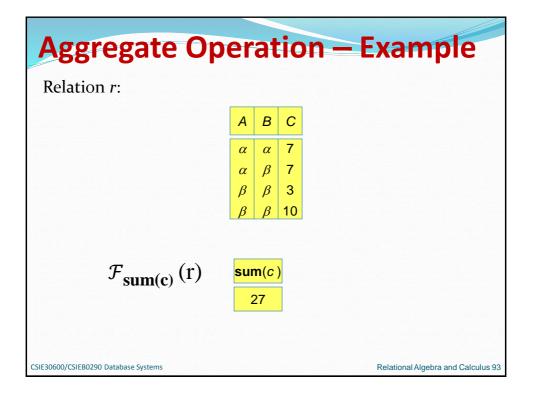


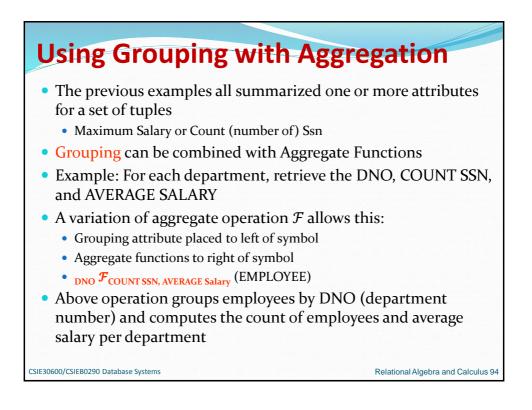


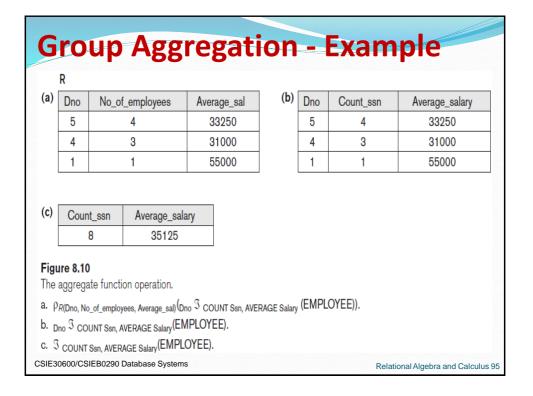




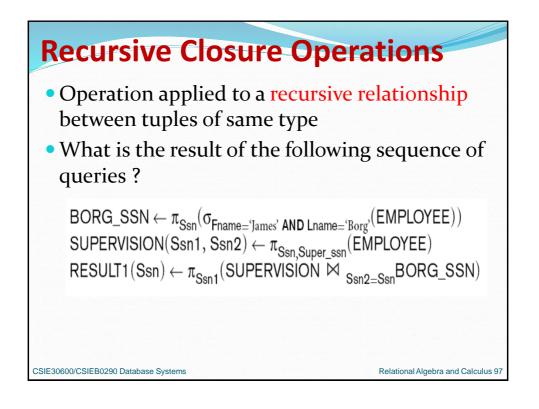


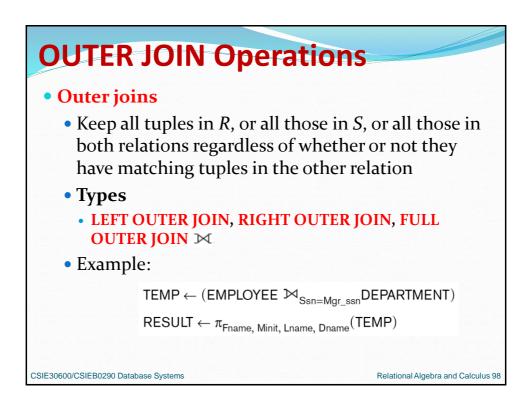


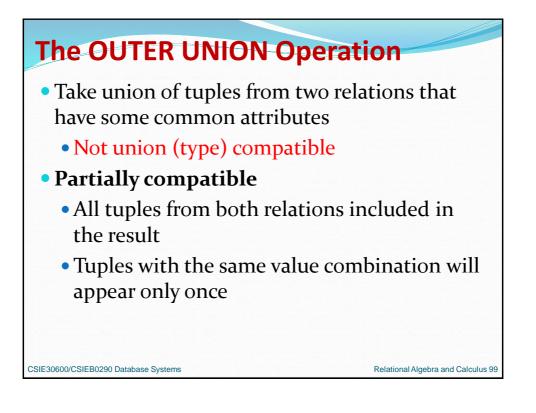


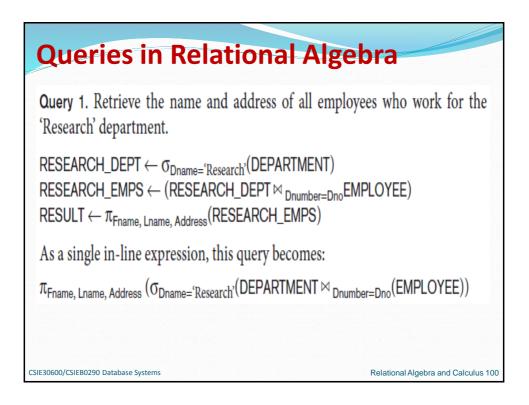


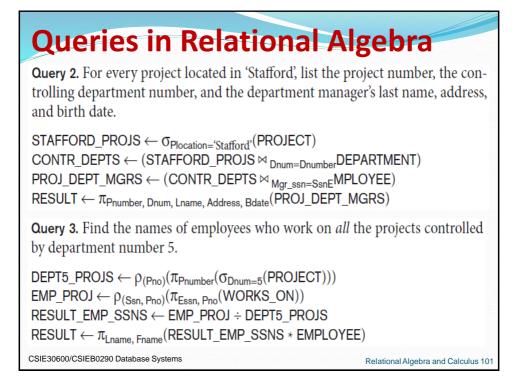
Aggregate Operation – More Example • Relation account grouped by branch-name:								
	branch_n	ame	account_	number	number balar			
	Perryridge Perryridge Brighton Brighton Redwood		A-102 A-201 A-217 A-215 A-222		400 900 750 750 750 700			
branch_name ${\mathcal F}_{{f sum}(balance)}$ (account)								
	brar			sum(ba	alance)			
	Perry Brigh Redu			13) 15) 70	00			
CSIE30600/CSIEB0290 Database	Systems					Relation	al Algebra and Calcul	us 96

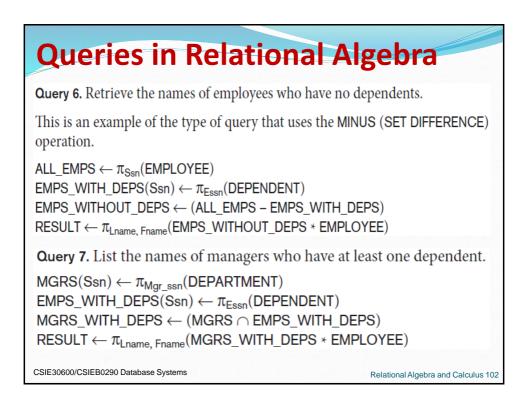


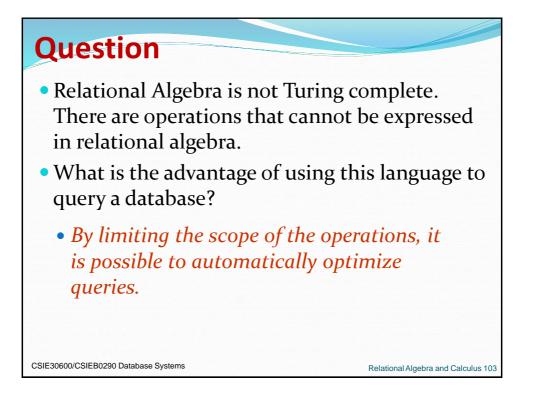


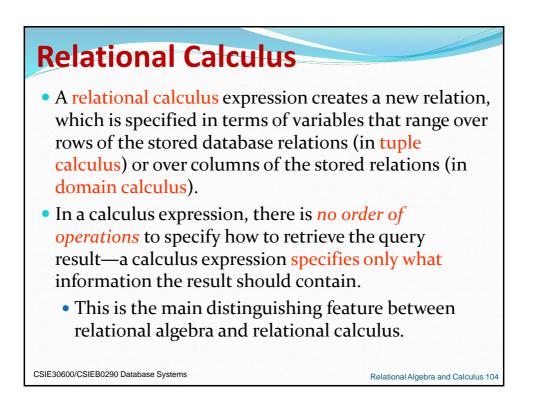


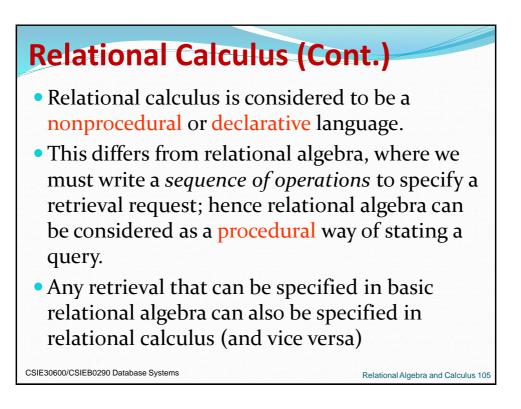


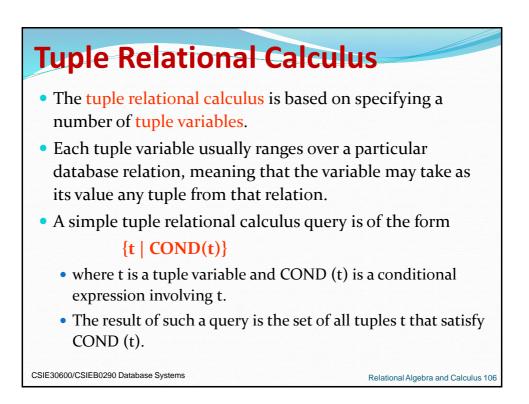


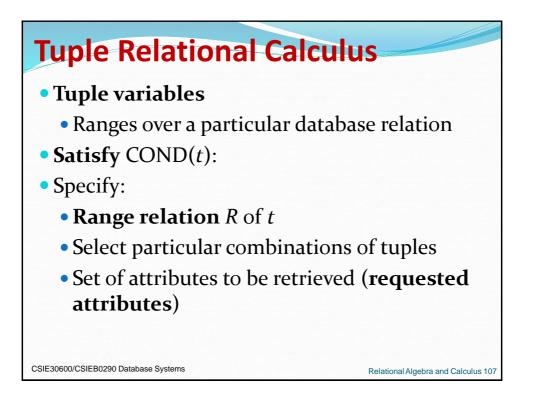


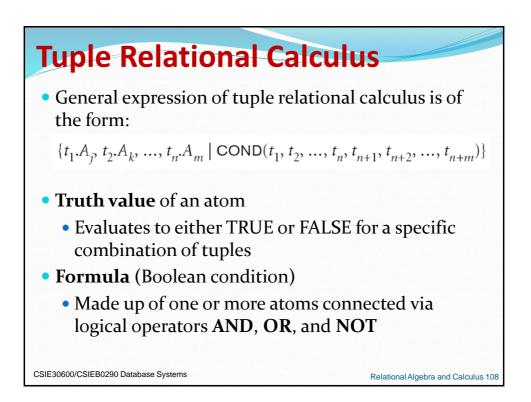


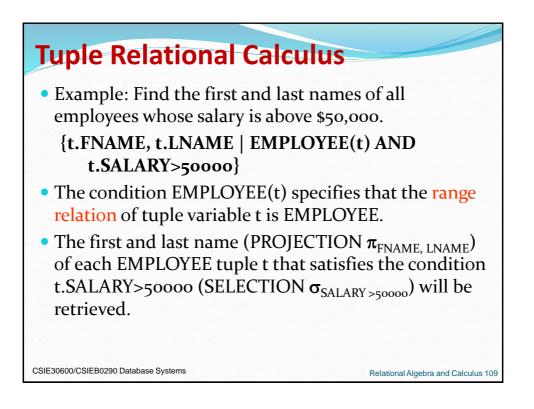


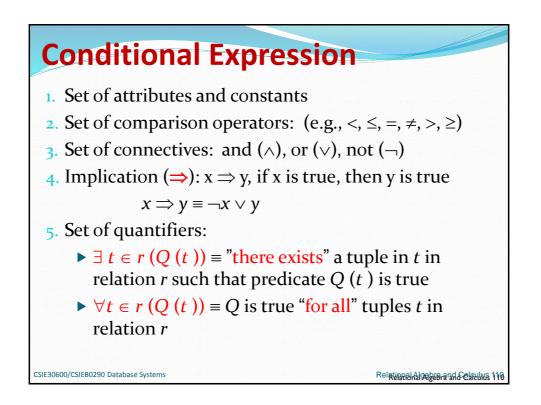


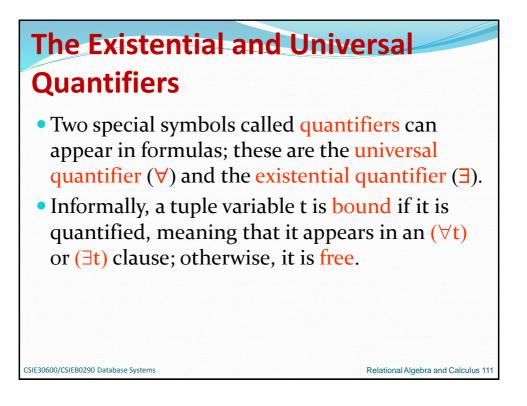


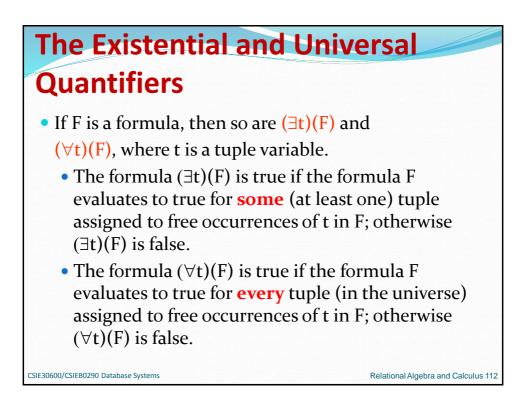


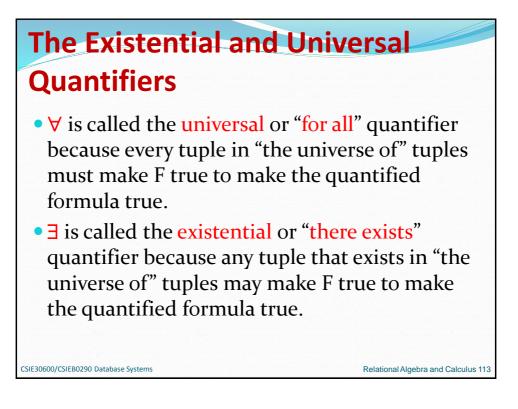












## **Example Query Using Existential** Quantifier

- The only *free tuple variables* in a relational calculus expression should be those that appear to the left of the bar ( | ).
  - In above query, t is the only free variable; it is then *bound successively* to each tuple.

**Query 1.** List the name and address of all employees who work for the 'Research' department.

**Q1:** {t.Fname, t.Lname, t.Address | EMPLOYEE(t) AND ( $\exists d$ )(DEPARTMENT(d) AND d.Dname='Research' AND d.Dnumber=t.Dno)}

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