

# CSIE30600/CSIEB0290 Database Systems

# Lecture 3: Relational Model

#### **Outline**



- Relational Model Concepts
- Relational Model Constraints
- Relational Database Schemas
- Update Operations
- Transactions
- Dealing with Constraint Violations

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#### **Data Model Revisited**



- Provides the means for specifying particular data structures, for constraining the data sets associated with these structures, and for manipulating the data
- Data definition language (DDL): define structures and constraints
- Data manipulation language (DML): specify manipulations/operations over the data

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Relational Model 3

#### Why Relational Model



- Extremely useful and simple
  - Single data-modeling concept: relations = 2-D tables
  - Allows clean yet powerful manipulation languages
- Most widely used model
  - Vendors: Oracle, IBM(DB2, Informix), Microsoft(SQL Server, Access), etc.
- Recent competitors: object-relational model, semi-structured model, document, key-value, NoSQL, NewSQL
  - MongoDB(document), Redis(key-value), Cassandra(NoSQL), HBase(NoSQL)
  - Object-oriented aspects of SQL:1999

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#### **Relational Model Concepts**



- The relational model of data is based on the concept of a relation
  - The strength of the relational approach to data management comes from the formal foundation provided by the theory of relations
- We review the essentials of the formal relational model in this chapter
- In practice, there is a standard model based on SQL – to be described in later lectures
- Note: There are several important differences between the *formal* model and the *practical* model, as we shall see

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#### **Relational Model Concepts**



- A relation is a mathematical concept based on sets
- The model was first proposed by Dr. E. F. Codd of IBM Research in 1970 in the following paper: (next slide)
  - "A Relational Model for Large Shared Data Banks,"
     Communications of the ACM, June 1970.
  - use relations as data structures, algebra for specifying queries, no mechanisms for updates or constraints
  - follow-up papers introduced new language based on first-order logic and showed it is equivalent to the algebra, introduced integrity constraints
- These papers caused a major revolution in the field of database management and earned Dr. Codd the coveted ACM Turing Award

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#### **Dawn of the Relational Model**



Information Retrieval

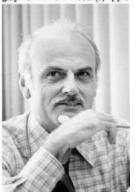
#### A Relational Model of Data for Large Shared Data Banks

E. F. Codd IBM Research Laboratory, San Jose, California

Future users of large data banks must be protected from having to know how the data is organized in the machine (the internal representation). A prompting service which supplies such information is not a satisfactory solution, Activities of users at terminals and most application programs should remain unaffected when the internal representation of data is changed and even when some aspects of the external representation are changed. Changes in data representation will often be needed as a result of changes in query, update, and report traffic and natural growth in the types of stored information.

Existing noninferential, formatted data systems provide users with tree-structured files or slightly more general network

The relational view (or model Section 1 appears to be superior ir graph or network model [3, 4] pre-



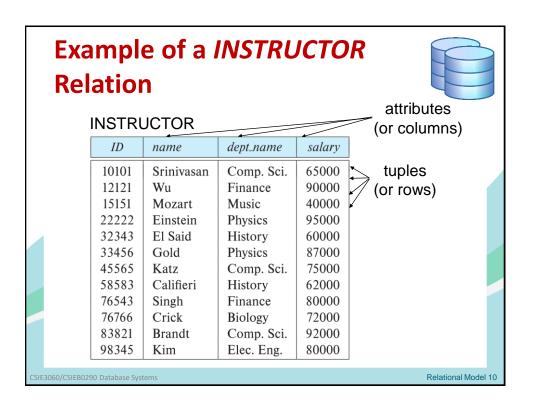
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#### **Informal Definitions**



- Informally, a relation looks like a table of values.
- A relation contains a set of rows.
- The data elements in each row represent certain facts that correspond to a real-world entity or relationship
  - In the formal model, rows are called tuples
- Each column has a column header that gives an indication of the meaning of the data in that column
  - In the formal model, the column header is called an attribute name (or just attribute)

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#### **Informal Definitions**



- **Key** of a Relation:
  - Each row has a value of a data item (or set of items) that uniquely identifies that row in the table
    - Called the key
  - In the INSTRUCTOR table, ID is the key
  - Sometimes row-ids or sequential numbers are assigned as keys to identify the rows
    - Called artificial key or surrogate key

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#### **Formal Definitions - Schema**



- The schema (or description) of a relation:
  - Denoted by R(A1, A2, .....An)
  - R is the name of the relation
  - The attributes of the relation are A1, A2, ..., An
  - The degree (or arity) of a relation: no. of attributes (n)
  - A relation instance r defined over schema R is denoted by r(R).
- Example: CUSTOMER(Cid, Cname, Address, Phone#)
  - CUSTOMER is the relation name
  - Defined over the 4 attributes: Cid, Cname, Address, Phone#
- Each attribute has a domain (a set of valid values)
  - For example, the domain of Cid is 6 digit numbers.
  - Denoted as dom(A1), dom(A2), ...

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## **Formal Definitions - Tuple**



- An n-tuple (row) is an ordered list of n values (enclosed in angled brackets  $\langle v_1, v_2, ..., v_n \rangle$ )
- Each value  $v_i$ ,  $1 \le i \le n$ , is an element of  $dom(A_i)$  or is a special NULL value (discussed later)
- Attribute values are atomic; that is, indivisible.
- A row in the CUSTOMER relation is a 4-tuple consisting of 4 values, for example:
  - <632895, "John Smith", "101 Main St. Atlanta, GA 30332", "(404) 894-2000">
- A relation r = {t<sub>1</sub>, t<sub>2</sub>, ..., t<sub>m</sub>} is a set of n-tuples

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#### **Formal Definitions - Domain**



- A domain has a logical definition:
  - Example: "USA\_phone\_numbers" are the set of 10 digit phone numbers valid in the U.S.
- A domain also has a data-type or a format defined for it.
  - The USA\_phone\_numbers may have a format: (ddd)ddd-dddd where each d is a decimal digit.
  - Dates have various formats such as year, month, date formatted as yyyy-mm-dd, or as dd mm,yyyy etc.

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## **Attribute Name and Domain**



- The attribute name designates the role played by a domain in a relation:
  - Used to interpret the meaning of the data elements corresponding to that attribute
  - Example: The domain Date may be used to define two attributes "Invoice-date" and "Payment-date"
- More example: attribute Cname is defined over the domain of char strings of max length 25
  - dom(Cname) is varchar(25)
- The role these strings play in the CUSTOMER relation is that of the *name of a customer*.

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#### **Relation State**



- The relation state is a subset of the Cartesian product of the domains of its attributes
- Each domain contains the set of all possible values the attribute can take.
- Cartesian product of the domains is the set of all possible combinations of attribute values (example in next slide)

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## **Relation State - Examples**



- Let R(A<sub>1</sub>, A<sub>2</sub>) be a relation schema:
  - Let dom(A<sub>1</sub>) = {0,1}
  - Let dom(A<sub>2</sub>) = {a,b,c}
- Cartesian product of the domains: dom(A<sub>1</sub>) × dom(A<sub>2</sub>) is all possible combinations:

- The relation state r(R) ⊂ dom(A₁) × dom(A₂)
- Eg.: r(R) could be {<0,a> , <0,b> , <1,c> }
  - this is one possible state (or "population" or "extension") r of the relation R, defined over A<sub>1</sub> and A<sub>2</sub>.
  - It has three 2-tuples: <0,a> , <0,b> , <1,c>

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#### **Formal Definitions - Summary**



- Formally,
  - Given  $R(A_1, A_2, ..., A_n)$
  - $r(R) \subset dom(A_1) \times dom(A_2) \times ... \times dom(A_n)$
- R(A<sub>1</sub>, A<sub>2</sub>, ..., A<sub>n</sub>) is the schema of the relation
- R is the name of the relation
- A<sub>1</sub>, A<sub>2</sub>, ..., A<sub>n</sub> are the attributes of the relation
- r(R): a specific state (or "value" or "population") of relation R – this is a set of tuples (rows)
  - $r(R) = \{t_1, t_2, ..., t_m\}$  where each  $t_i$  is an n-tuple
  - ti =  $\langle v_1, v_2, ..., v_n \rangle$  where each  $v_j$  is an *element-of* dom(A<sub>j</sub>)

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#### **Definition Summary**



Informal Terms	Formal Terms
Table	Relation
Column Header	Attribute
All possible Column Values	Domain
Row	Tuple
Table Definition	Schema of a Relation
Populated Table	State of the Relation

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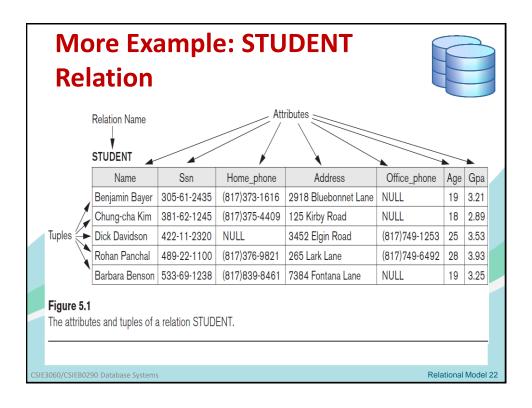
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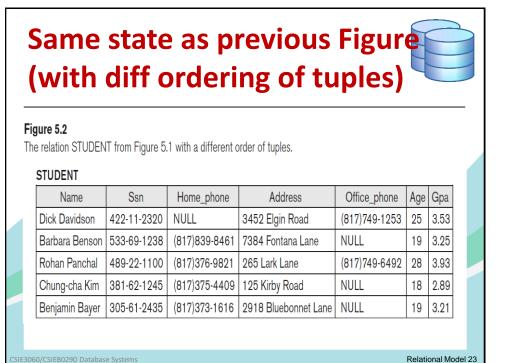
## **Characteristics Of Relations**



- Ordering of tuples in a relation r(R):
  - The tuples are NOT ordered, even though they appear to be in the tabular form.
- Ordering of attributes in a relation schema R (and of values within each tuple):
  - -Attributes in R(A<sub>1</sub>, A<sub>2</sub>, ..., A<sub>n</sub>) and the values in t= $\langle v_1, v_2, ..., v_n \rangle$  are ordered.

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# **Characteristics of Relations**



- Values in tuples:
  - All values are considered atomic (indivisible).
  - Each value in a tuple must be from the domain of the attribute for that column
    - If tuple t = < v<sub>1</sub>, v<sub>2</sub>, ..., v<sub>n</sub> > is a tuple (row) in the relation state r of R(A<sub>1</sub>, A<sub>2</sub>, ..., A<sub>n</sub>)
    - Then each  $v_i$  must be a value from  $dom(A_i)$
  - Flat relational model
    - Composite and multivalued attributes not allowed
    - First normal form assumption

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#### **NULL**



- NULL values
  - A special NULL value is used to represent values that are unknown or inapplicable.
- Meanings for NULL values:
  - Value unknown
  - Value exists but is not available
  - Attribute does not apply to this tuple (also known as value undefined)
- The null value causes complications in the definition of many operations.

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# **Characteristics of Relations**



- Interpretation (meaning) of a relation
  - Assertion
    - Each tuple in the relation is a fact or a particular instance of the assertion
  - Predicate
    - Values in each tuple interpreted as values that satisfy predicate

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#### **Relational Model Notation**



- Relation schema R of degree n
  - Denoted by  $R(A_1, A_2, ..., A_n)$
- Uppercase letters Q, R, S
  - Denote relation names
- Lowercase letters q, r, s
  - Denote relation states
- Letters t, u, v
  - Denote tuples

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#### **Relational Model Notation**



- We refer to component values of a tuple t by:
  - $-t[A_i]$  or  $t.A_i$
  - -This is the value v<sub>i</sub> of attribute A<sub>i</sub> for tuple t
- Similarly, t[A<sub>u</sub>, A<sub>v</sub>, ..., A<sub>w</sub>] and t(A<sub>u</sub>, A<sub>v</sub>, ..., A<sub>w</sub>) refers to the subtuple of t containing the values of attributes A<sub>u</sub>, A<sub>v</sub>, ..., A<sub>w</sub>, respectively in t

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#### **Relational Model Constraints**



- Constraints
  - Restrictions on the actual values in a database state
  - Derived from the rules in the miniworld that the database represents
  - Must hold on all valid relation states.
  - Three categories (below)
- Inherent model-based constraints or implicit constraints
  - Inherent in the data model

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#### **Relational Model Constraints**

- Schema-based constraints or explicit constraints
  - Can be directly expressed in schemas of the data model
- Application-based or semantic constraints or business rules
  - Cannot be directly expressed in schemas
  - Expressed and enforced by application program

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#### **Domain Constraints**



- An implicit constraint is the domain constraint
  - Every value in a tuple must be from the domain of its attribute (or null, if allowed for that attribute)
- Typically include:
  - Numeric data types for integers and real numbers
  - Characters
  - Booleans
  - Fixed-length strings
  - Variable-length strings
  - Date, time, timestamp
  - Money
  - Other special data types

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#### **Key Constraints**

- No two tuples can have the same combination of values for all their attributes. (no duplicate tuples)
- Superkey of R is a set of attributes SK of R such that:
  - No two tuples in any valid state r(R) will have the same value for SK (can uniquely identify tuples)
  - That is, for any distinct tuples t1 and t2 in r(R), t1[SK] ≠ t2[SK]
  - This condition must hold in any valid state r(R)
- Key (candidate key) of R:
  - A "minimal" superkey
  - A key is a superkey K such that removal of any attribute from K results in a set of attributes that is not a superkey (does not possess the superkey uniqueness property)

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# **Key Constraints (continued)**



- Example: Consider the CAR relation schema:
  - CAR(State, Reg#, SerialNo, Make, Model, Year)
    - CAR has two keys:
      - Key1 = {State, Reg#}
      - Key2 = {SerialNo}
    - Both are also superkeys of CAR
  - {SerialNo, Make} is a superkey but not a key. (why?)
- In general:
  - Any key is a superkey (but not vice versa)
  - Any set of attributes that includes a key is a superkey
  - A minimal superkey is also a key

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#### **Examples of Keys**



- Example: Consider the STUDENTS schema STUDENTS(SSN, StuID, Name, Major, Bdate)
- What are the candidate keys of STUDENTS?
- What is the primary key?
- Is (Name, Major) a superkey?
- What about (SSN, Name)?
- Is (SSN, Name) a candidate key? Why(not)?

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#### **Key Constraints (continued)**



- A relation can have several candidate keys
- Primary key of the relation
  - A designated key among candidate keys
  - Underline attribute
- Example: Consider the CAR relation schema:
  - CAR(State, Reg#, SerialNo, Make, Model, Year)
  - We choose SerialNo as the primary key
- Other candidate keys are also known as unique keys

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# **Key Constraints (continued)**



- The primary key value is used to uniquely identify each tuple in a relation
  - Provides the tuple identity
- Also used to reference the tuple from another relation
  - General rule: Choose as primary key the smallest of the candidate keys (in terms of size)
  - Not always applicable choice is sometimes subjective

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# CAR table with two candidate keys – LicenseNumber chosen as Primary Key



CAR

Figure 5.4
The CAR relation, with two candidate keys:
License\_number and
Engine\_serial\_number.

License_number	Engine_serial_number	Make	Model	Year
Texas ABC-739	A69352	Ford	Mustang	02
Florida TVP-347	B43696	Oldsmobile	Cutlass	05
New York MPO-22	X83554	Oldsmobile	Delta	01
California 432-TFY	C43742	Mercedes	190-D	99
California RSK-629	Y82935	Toyota	Camry	04
Texas RSK-629	U028365	Jaguar	XJS	04

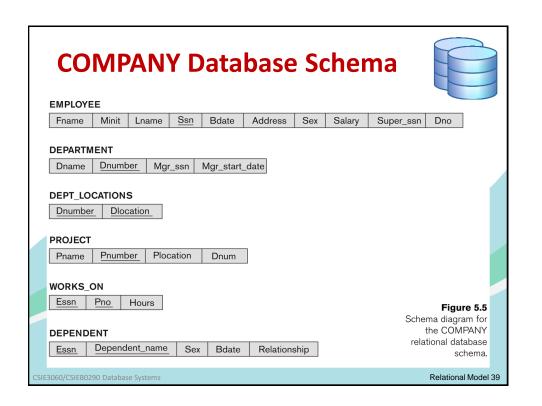
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#### **Database Schema & State**



- Relational Database Schema:
  - A set  $\mathbf{S} = \{R_1, R_2, ..., R_n\}$  of relation schemas that belong to the same database.
  - A set of integrity constraints IC
- Following slide shows a COMPANY database schema with 6 relation schemas
- Relational database state
  - Set of relation states **DB** =  $\{r_1, r_2, ..., r_m\}$
  - Each  $r_i$  is a state of  $R_i$  and such that the  $r_i$  relation states satisfy integrity constraints specified in IC

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# **Relational Database State**



- Valid state
  - Satisfies all the constraints in the defined set of integrity constraints IC
- Invalid state
  - Does not obey all the integrity constraints

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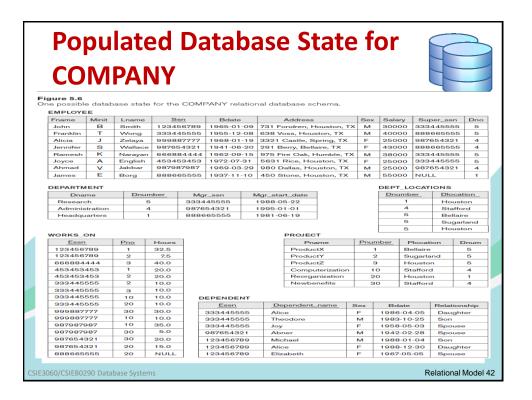
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#### **Populated Database State**



- Each relation has tuples in its current relation state
- The relational database state is a union of all the individual relation states
- Whenever the database is changed, a new state arises
- Basic operations for changing the database:
  - INSERT a new tuple in a relation
  - DELETE an existing tuple from a relation
  - MODIFY an attribute of an existing tuple
- Next slide shows an example state for the COMPANY database

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#### **Entity Integrity**



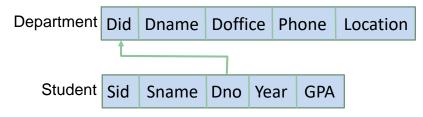
- The primary key attributes PK of each relation schema R in S cannot have null values in any tuple of r(R).
  - This is because primary key values are used to identify the individual tuples.
  - $-t[PK] \neq null$  for any tuple t in r(R)
  - If PK has several attributes, null is not allowed in any of these attributes
- Note: Other attributes of R may be constrained to disallow null values, even though they are not members of the primary key.

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#### **Referential Integrity**



- A constraint involving two relations
  - The previous constraints involve a single relation.
- Used to specify a relationship among tuples in two relations:
  - The referencing relation and the referenced relation.
  - Maintains consistency among tuples in two relations



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#### **Referential Integrity**



- Tuples in the referencing relation R1 have attributes
   FK (called foreign key) that reference the primary key attributes PK of the referenced relation R2.
  - Value of FK in a tuple t1 of the current state r1(R1) either occurs as a value of PK for some tuple t2 in the current state r2(R2) or is NULL.
  - t1 is said to **reference** t2 if t1 [FK] = t2 [PK].
- A referential integrity constraint can be displayed in a relational database schema as a directed arc from R1.FK to R2.

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# Referential Integrity (or foreign key) Constraint



- Statement of the constraint
  - The value in the foreign key column (or columns)
     FK of the referencing relation R1 can be either:
    - (1) a value of an existing primary key value of a corresponding primary key PK in the referenced relation R2, or
    - (2) a null.
- In case (2), the FK in R1 should not be a part of its own primary key.

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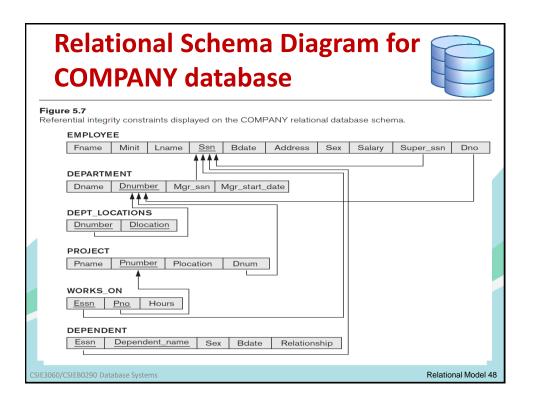
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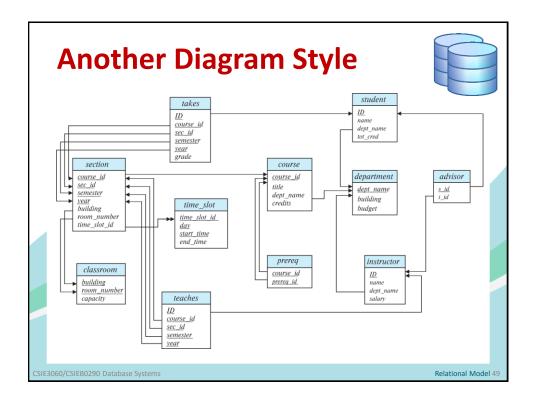
# Displaying a Schema and Constraints



- Each relation schema can be displayed as a row of attribute names
- The name of the relation is written above the attribute names
- The primary key attribute (or attributes) will be underlined
- A foreign key (referential integrity) constraints is displayed as a directed arc (arrow) from the foreign key attributes to the referenced table
  - Can also point the the primary key of the referenced relation for clarity
- Next slide shows the COMPANY relational schema diagram

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#### **Other Types of Constraints**



- Semantic integrity constraints
  - based on application semantics and cannot be expressed by the model per se
  - Example: "the max. no. of hours per employee for all projects is 56 hrs per week"
- A constraint specification language may have to be used to express these
- SQL allows triggers and assertions to express for some of these
  - More common to check for these types of constraints within the application programs

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#### **Other Types of Constraints**



- Functional dependency constraint
  - Establishes a functional relationship among two sets of attributes X and Y
  - Value of X determines a unique value of Y
- State constraints
  - Define the constraints that a valid state of the database must satisfy
- Transition constraints
  - Define to deal with state changes in the database

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# Specification of a Relational Schema



- Select the relations, with a name for each table
- Select attributes for each relation and give the domain for each attribute
- Specify the key(s) for each relation
- Specify all appropriate foreign keys and integrity constraints
- Database schema is the set of schemas for the relations in a design

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#### **Update Operations on Relations**



- Basic operations that change the states of relations in the database:
  - Insert, Delete, Update (or Modify)
- Integrity constraints should not be violated by the update operations.
- Several update operations may have to be grouped together.
- Updates may propagate to cause other updates automatically. This may be necessary to maintain integrity constraints.

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#### **Update Operations on Relations**

- In case of integrity violation, several actions can be taken:
  - Cancel the operation that causes the violation (RESTRICT or REJECT option)
  - Perform the operation but inform the user of the violation
  - Trigger additional updates so the violation is corrected (CASCADE option, SET NULL option)
  - Execute a user-specified error-correction routine

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#### **The Insert Operation**



- Provides a list of attribute values for a new tuple t that is to be inserted into a relation R
- INSERT may violate any of the constraints:
  - Domain constraint:
    - if one of the attribute values provided for the new tuple is not of the specified attribute domain
  - Key constraint:
    - if the value of a key attribute in the new tuple already exists in another tuple in the relation
  - Referential integrity:
    - if a foreign key value in the new tuple references a primary key value that does not exist in the referenced relation
  - Entity integrity:
    - if the primary key value is null in the new tuple

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#### **The Delete Operation**



- DELETE may violate only referential integrity:
  - If the primary key value of the tuple being deleted is referenced from other tuples
    - Can be remedied by several actions: RESTRICT, CASCADE, SET NULL or SET DEFAULT (will discuss)
      - RESTRICT option: reject the deletion
      - CASCADE option: propagate the new primary key value into the foreign keys of the referencing tuples
      - SET option: set the foreign keys of the referencing tuples to NULL or default value
  - One of the above options must be specified during database design for each foreign key constraint

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#### **The Update Operation**



- Need to specify a condition on attributes of relation
  - Select the tuple (or tuples) to be modified
- UPDATE may violate domain constraint and NOT NULL constraint on an attribute being modified
- Any of the other constraints may also be violated, depending on the attribute being updated:
  - Updating the primary key (PK):
    - Similar to a DELETE followed by an INSERT
    - Need to specify similar options to DELETE
  - Updating a foreign key (FK):
    - · May violate referential integrity
  - Updating an ordinary attribute (neither PK nor FK):
    - · Can only violate domain constraints

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## **The Transaction Concept**



- Transaction
  - Executing a designated function
  - Includes a sequence of operations
  - Considered as a single composite operation
  - Must leave the database in a valid or consistent state
- Online transaction processing (OLTP) systems
  - Execute transactions at rates that reach several hundred per second

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#### Summary



- Relational model concepts
  - Definitions (informal and formal)
  - Characteristics of relations
- Relational model constraints and database schemas
  - Inherent model-based constraints, explicit schema-based constraints, and application-based constraints
  - Domain constraints, Key constraints, Entity integrity, Referential integrity
- Relational update operations and dealing with constraint violations

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#### **Exercise**



Consider the following relations for a database that keeps track of student enrollment in courses and the books adopted for each course:

STUDENT(SSN, Name, Major, Bdate)

COURSE(Course#, Cname, Dept)

ENROLL(SSN, Course#, Quarter, Grade)

BOOK\_ADOPTION(Course#, Quarter, Book\_ISBN)

TEXT(Book\_ISBN, Book\_Title, Publisher, Author)

Draw a relational schema diagram specifying the foreign keys for this schema.

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